

Mutual Impedance Modeling for BepiColombo: Including Ion Dynamics Effects

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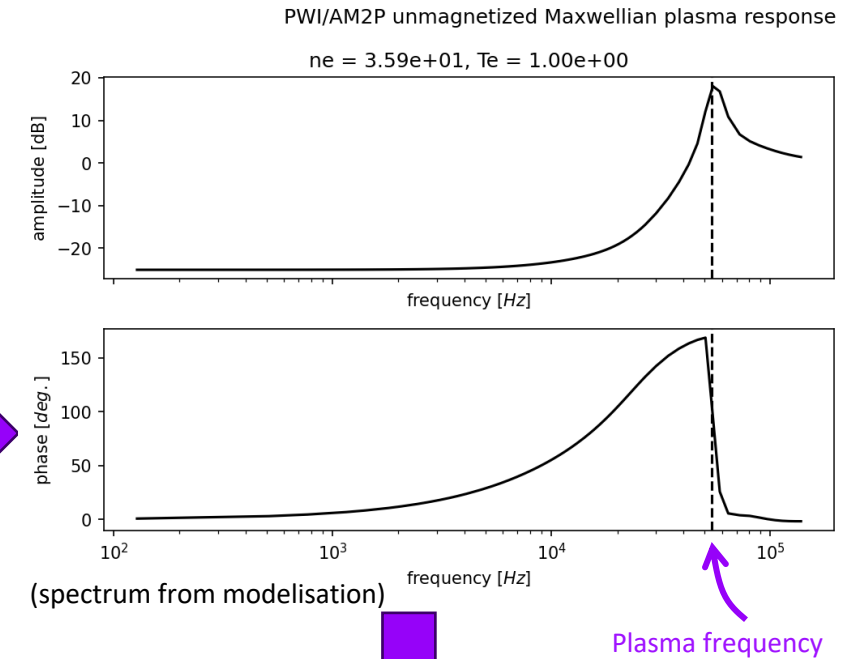


Context

BepiColombo will arrive **end of 2026** at Mercury

PWI/AM²P antennas
developped by LPC2E
(uses MEFISTO Swedish
antennas)

**Mutual impedance
measurements**
to probe the plasma
surrounding Mercury

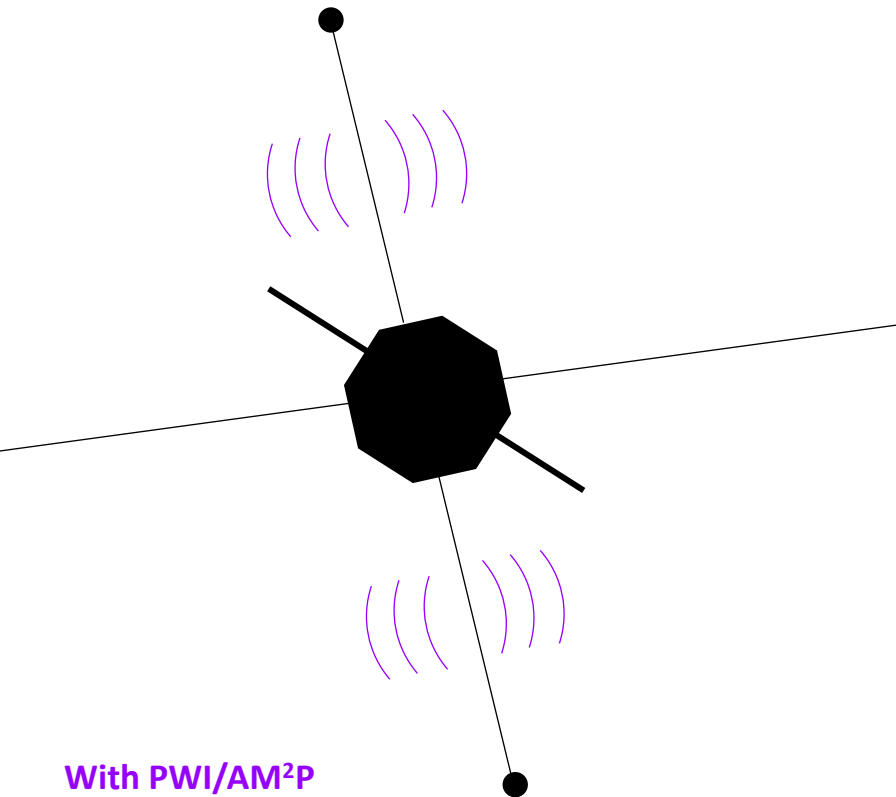


We deduce:
Electron density n_e
Electron temperature T_e
+ if multiple electron populations exist

Mutual Impedance

Measurement principle:

1. Current emitted by the emitting wires at a frequency ω



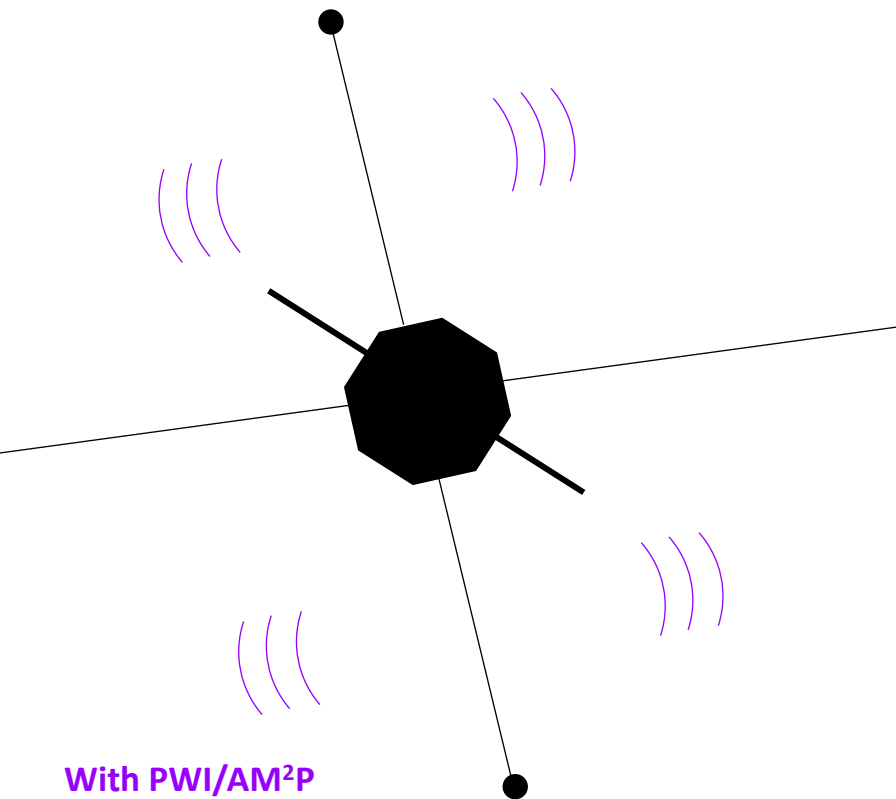
With PWI/AM²P
onboard BepiColombo



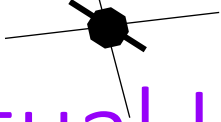
Mutual Impedance

Measurement principle:

1. Current emitted by the emitting wires at a frequency ω
2. The signal is propagating through the plasma $\rightarrow$ dielectric response



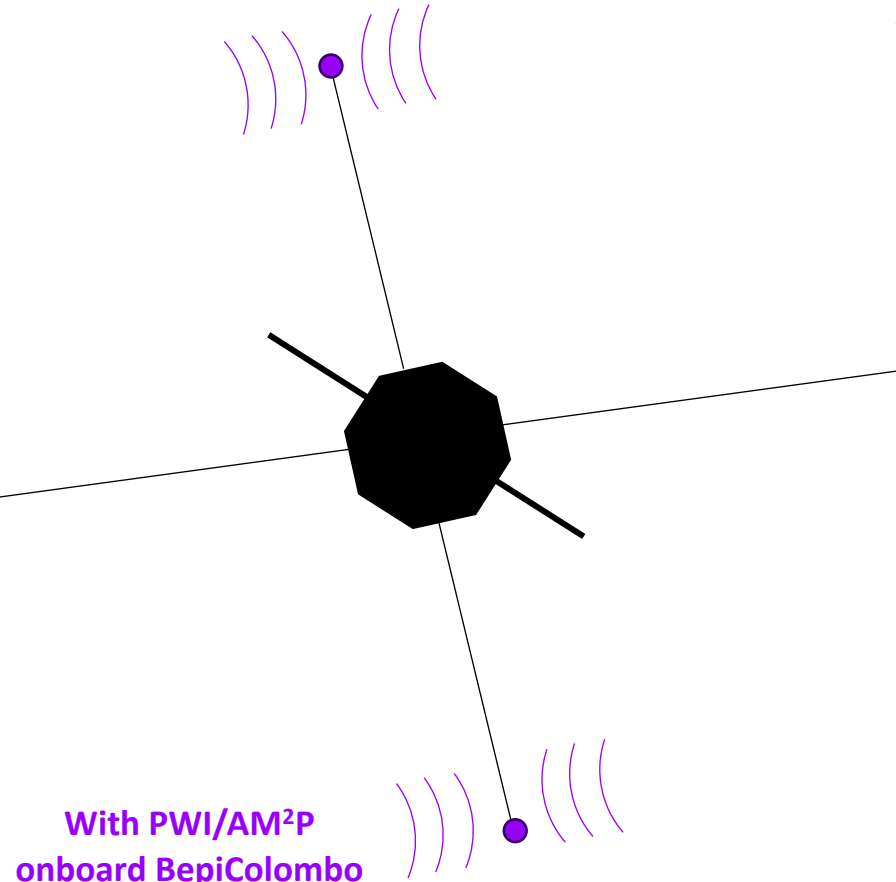
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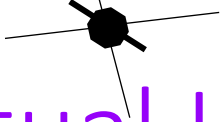


Mutual Impedance

Measurement principle:

1. Current emitted by the emitting wires at a frequency ω
2. The signal is propagating through the plasma $\rightarrow$ dielectric
3. We measure the potential seen by the receiving spheres



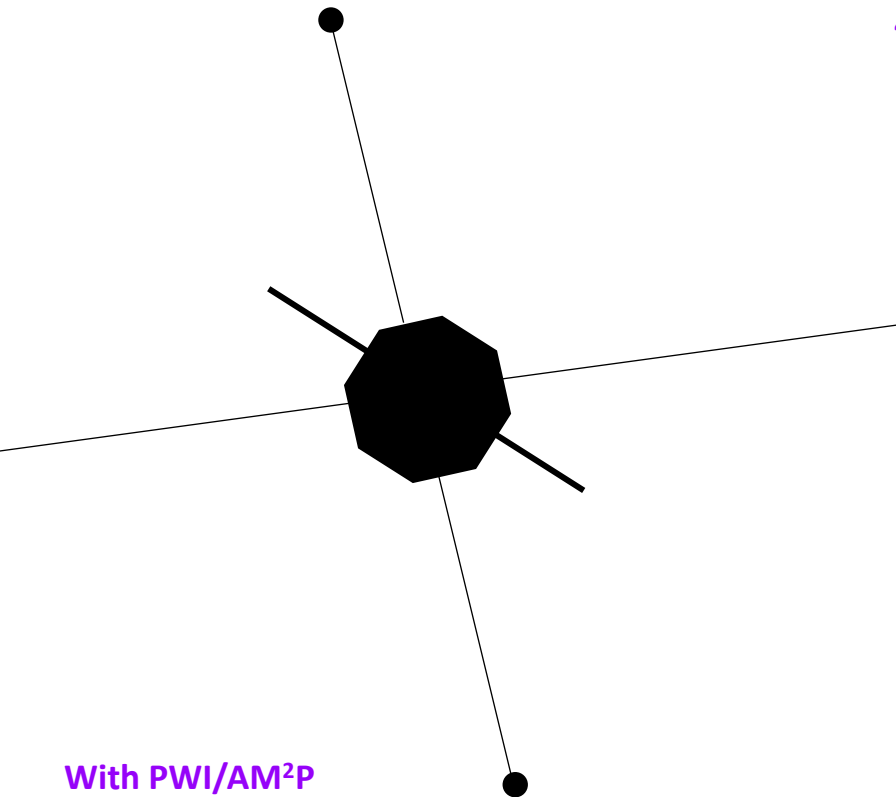


Mutual Impedance

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4. We calculate the mutual impedance $H(\omega)$:

$$H(\omega) = \frac{\Delta Z}{\Delta Z_0} = \frac{V_{R_2}(\omega) - V_{R_1}(\omega)}{V_{R_2,0} - V_{R_1,0}}$$



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At several frequencies:

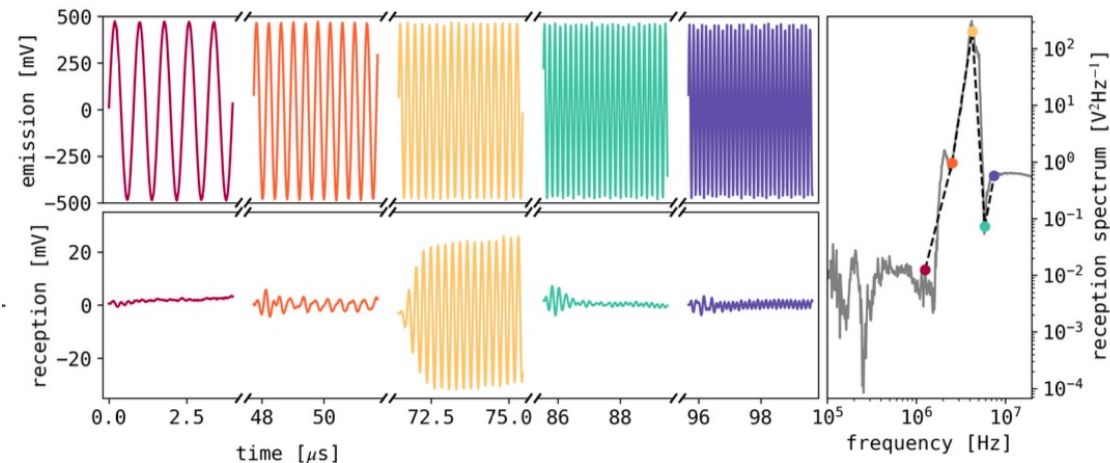


Fig. from P. Dazzi's thesis (2025)

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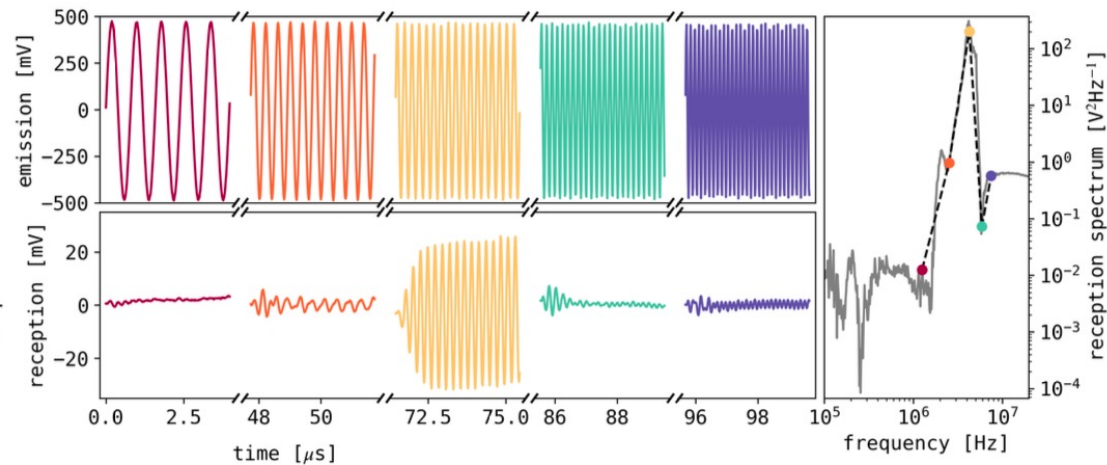


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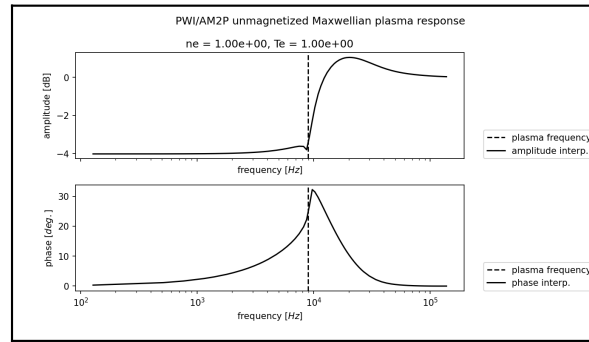
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Mutual Impedance

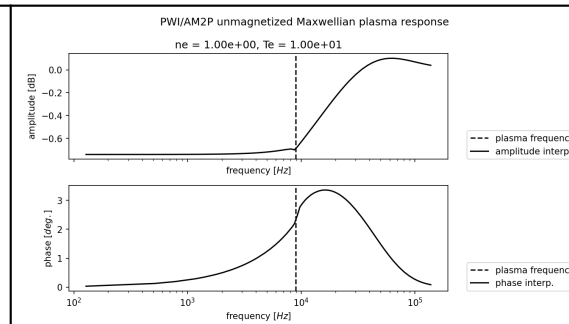
$T_e =$
 $n_e =$

1 cm^{-3}

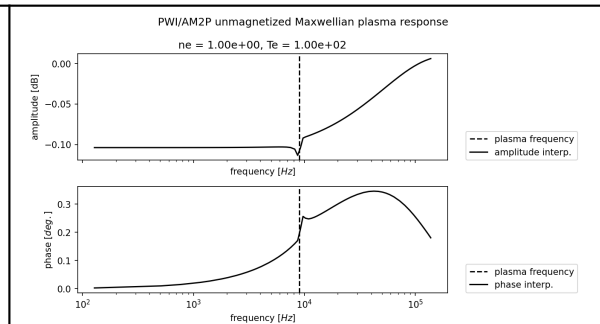
1 eV



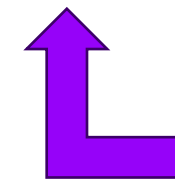
10 eV



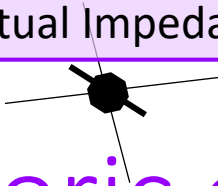
100 eV



Spectrum shape depends on electron temperature
→ inverse problem

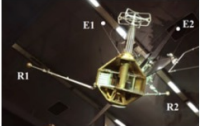
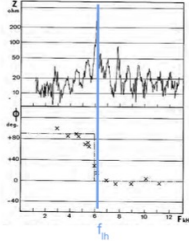
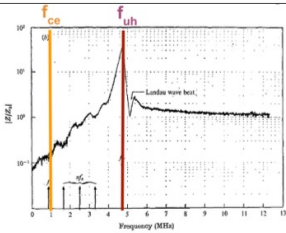


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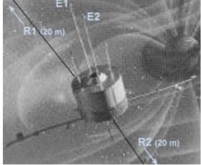
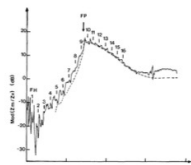
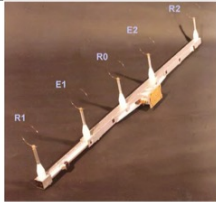
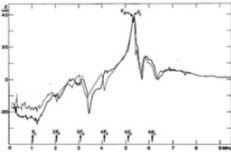
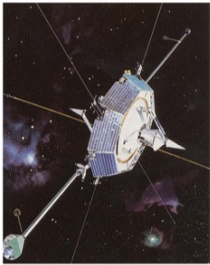
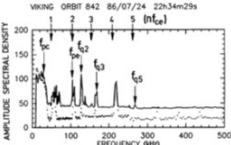
Historic of Mutual Impedance

Rocket sounding since 1969

Instrument	Géométrie	Exemple de données
Sonde quadripolaire à bord de la fusée French FR-1 [Storey et al., 1969]		
Sonde quadripolaire à bord de la fusée DRAGON-3 [Beghin, 1971]		
Sonde CISASPE à bord d'une fusée Véronique [Chassériaux et al., 1972]		

Tables from N. Gilet's thesis (2017)

Onboard satellites since 1978

Instrument	Géométrie	Exemple de données
Sonde S-304 à bord de GEOS-1 [Décréau et al., 1978a]		
Sonde ISOBPROBE-3 à bord de ARCAD-3 [Beghin et al., 1982]		
Sonde à bord du satellite Viking [Bahnsen et al., 1986; Perraut et al., 1990]		
Sonde PWA à bord du satellite HUYGENS [Hamelin et al., 2007]		



Historic of Mutual Impedance

Recent space missions equipped with mutual impedance:

Instrument RPC-MIP, onboard Rosetta,
on 67P comet (up to 2016)

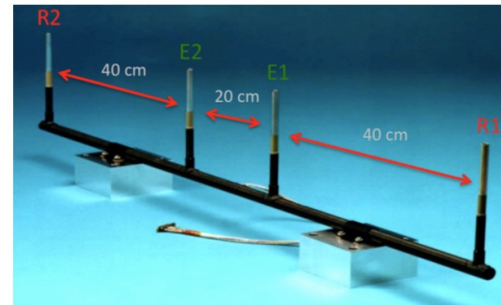
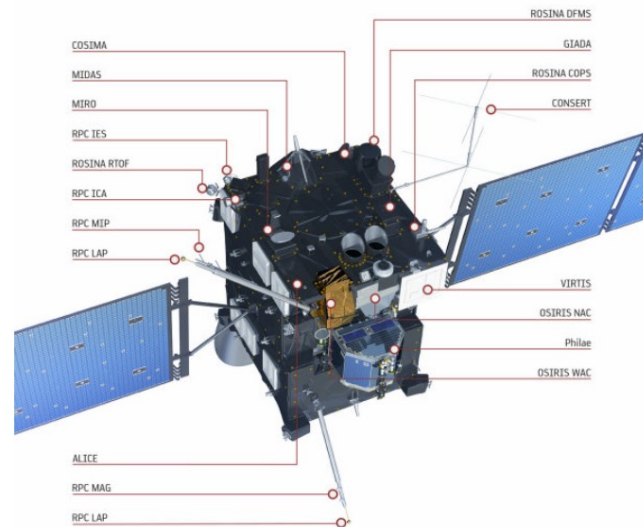
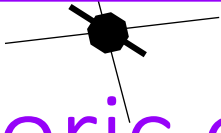


FIGURE 2.8 – La sonde à impédance mutuelle RPC-MIP à bord du satellite spatial *Rosetta*: sonde d'un mètre de long possédant deux émetteurs E_1 et E_2 et deux récepteurs, R_1 et R_2 à ses extrémités. Adaptée de Trotignon et al. [2007].

(Crédit : ESA/Science)

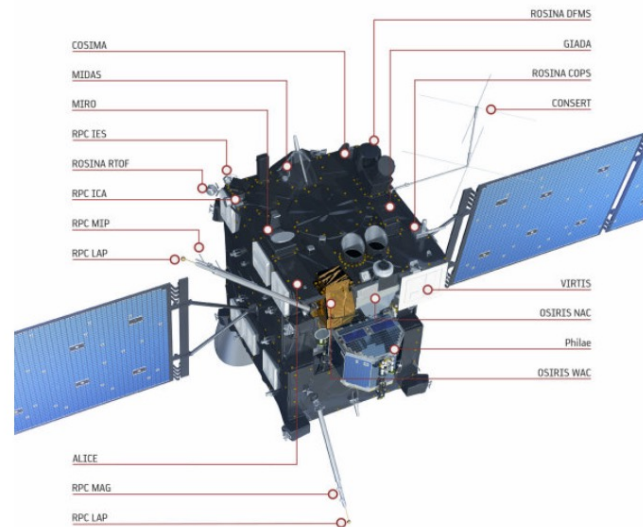
Figure from N. Gilet's thesis (2017)



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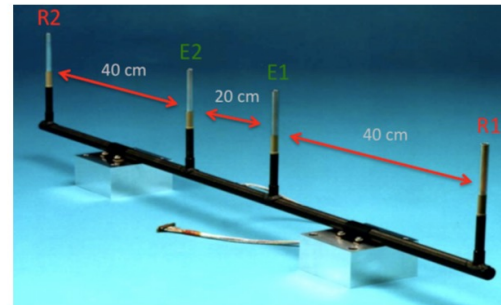
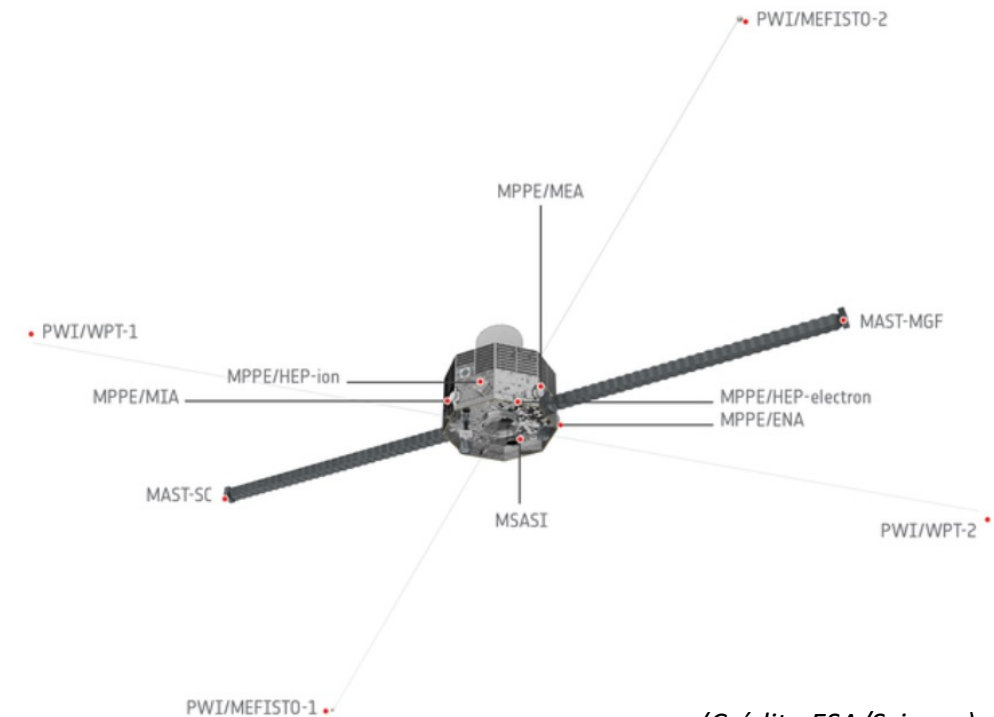


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Figure from N. Gilet's thesis (2017)

Instrument PWI/AM2P, onboard BepiColombo,
soon around Mercury (in 2027)



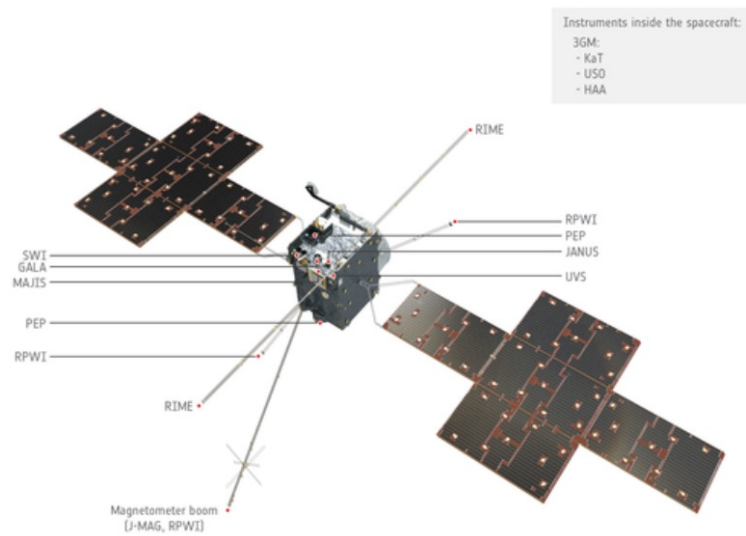
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Historic of Mutual Impedance

Recent/future space missions equipped with mutual impedance:

Instrument RPWI/MIME, onboard JUICE,
around Jupiter and his moons (from 2031)

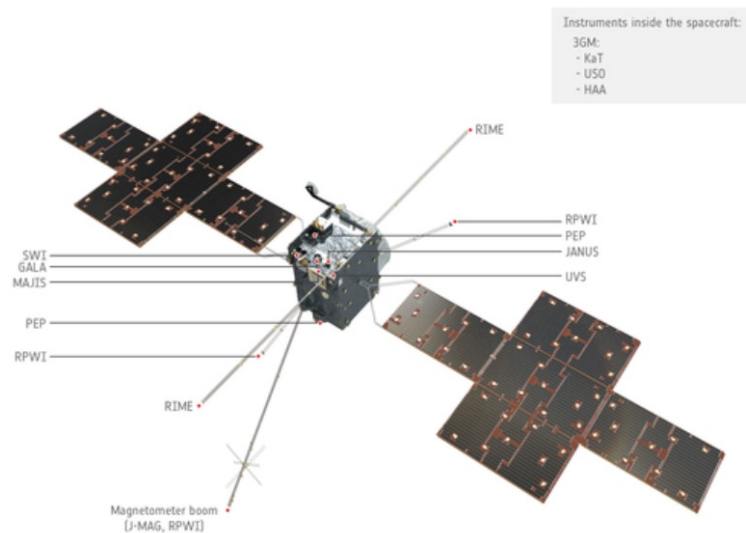


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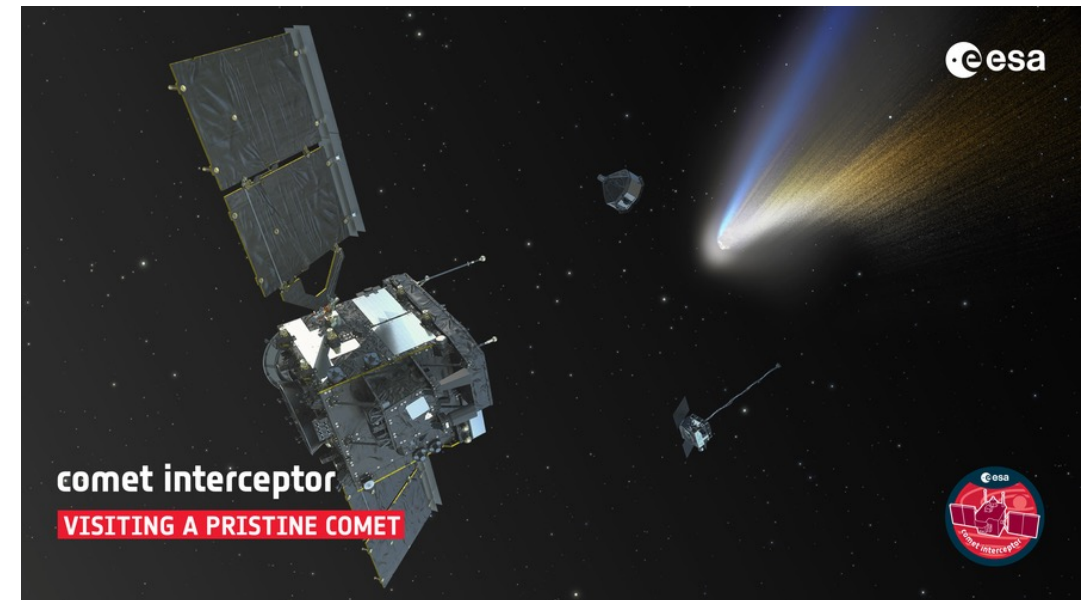
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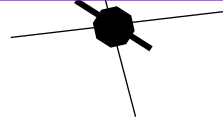
Instrument RPWI/MIME, onboard JUICE,
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(Crédit : ESA/Science)

Instrument DFP/Compliment, onboard Comet Interceptor,
through a pristine comet (launch ~2029)

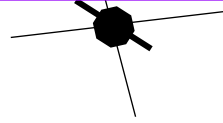




Objectives

Prepare the BepiColombo future data

- Diagnostic of electron populations



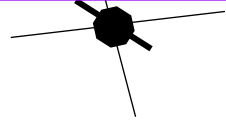
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But also:

- Try to make a diagnostic of **ions** *in some configurations!*



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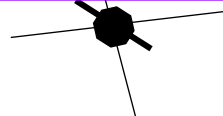
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Why?

- the response is dominated by electrons
- ions oscillate at lower frequencies
→ frequencies not in the instrumental frequency range



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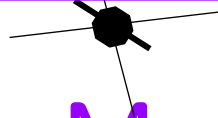
How:

We need to add the ion contribution in AM²P response model

Instrumental Response Modeling of Mutual Impedance

We measure: $V_R(\omega)$

which depends on: $\varepsilon(k, \omega)$



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We need to calculate $\varepsilon(k, \omega)$ theoretically:

Vlasov +
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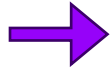
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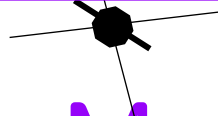
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Linearisation
+ Fourier

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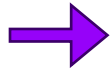


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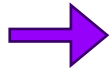
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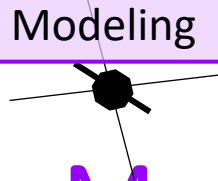
Linearisation
+ Fourier



Use Maxwellian
velocity
function

$$\begin{cases} \frac{\partial f}{\partial t}(\mathbf{x}, \mathbf{v}, t) + \mathbf{v} \cdot \nabla_{\mathbf{x}} f(\mathbf{x}, \mathbf{v}, t) + \frac{e}{m_e} \mathbf{E} \cdot \nabla_{\mathbf{v}} f(\mathbf{x}, \mathbf{v}, t) = 0 \\ \nabla \cdot \mathbf{E} = \frac{e}{\varepsilon_0} \int f(\mathbf{x}, \mathbf{v}, t) d\mathbf{v} \end{cases}$$

$$f_0(\mathbf{v}) = \left(\frac{m_e}{2\pi k_B T_e} \right)^{3/2} e^{-m_e |\mathbf{v}|^2 / 2 k_B T}$$

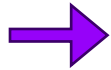


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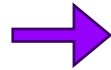
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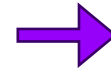
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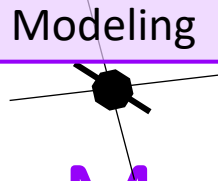


Calculate
dielectric
 $\varepsilon(k, \omega)$

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$$\varepsilon_l(k, \omega) = 1 - \frac{\omega_{pe}^2}{k^2} \int \frac{v}{\sqrt{2\pi} v_{th}^3} \frac{e^{\frac{v^2}{2v_{th}^2}}}{\frac{\omega}{k} - v} dv$$

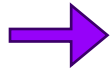


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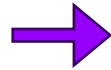
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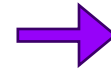
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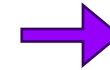
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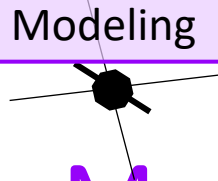
Calculate the
wave potential
 V/V_0

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$$\phi(\omega, r) = \frac{Q}{4\pi\varepsilon_0} \frac{2}{\pi} \lim_{\text{Im}(\omega) \rightarrow 0} \int_0^{+\infty} \frac{\sin(kr)}{kr} \frac{dk}{\varepsilon_l(\omega, k)}$$

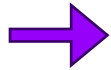


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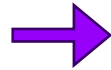
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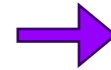
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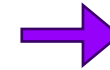
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Calculate
dielectric
 $\varepsilon(k, \omega)$



Calculate the
wave potential
 V/V_0



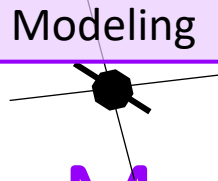
Already modelised by a
fortran code
(written by N. Gilet)

$$\begin{cases} \frac{\partial f}{\partial t}(\mathbf{x}, \mathbf{v}, t) + \mathbf{v} \cdot \nabla_{\mathbf{x}} f(\mathbf{x}, \mathbf{v}, t) + \frac{e}{m_e} \mathbf{E} \cdot \nabla_{\mathbf{v}} f(\mathbf{x}, \mathbf{v}, t) = 0 \\ \nabla \cdot \mathbf{E} = \frac{e}{\varepsilon_0} \int f(\mathbf{x}, \mathbf{v}, t) d\mathbf{v} \end{cases}$$

$$f_0(\mathbf{v}) = \left(\frac{m_e}{2\pi k_B T_e} \right)^{3/2} e^{-m_e |\mathbf{v}|^2 / 2 k_B T}$$

$$\varepsilon_l(k, \omega) = 1 - \frac{\omega_{pe}^2}{k^2} \int \frac{v}{\sqrt{2\pi} v_{th}^3} \frac{e^{\frac{v^2}{2v_{th}^2}}}{\frac{\omega}{k} - v} dv$$

$$\phi(\omega, r) = \frac{Q}{4\pi\varepsilon_0} \frac{2}{\pi} \lim_{\text{Im}(\omega) \rightarrow 0} \int_0^{+\infty} \frac{\sin(kr)}{kr} \frac{dk}{\varepsilon_l(\omega, k)}$$

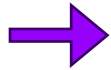


Instrumental Response Modeling of Mutual Impedance

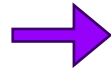
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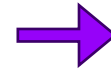
Vlasov +
Poisson
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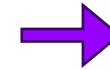
Linearisation
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Use Maxwellian
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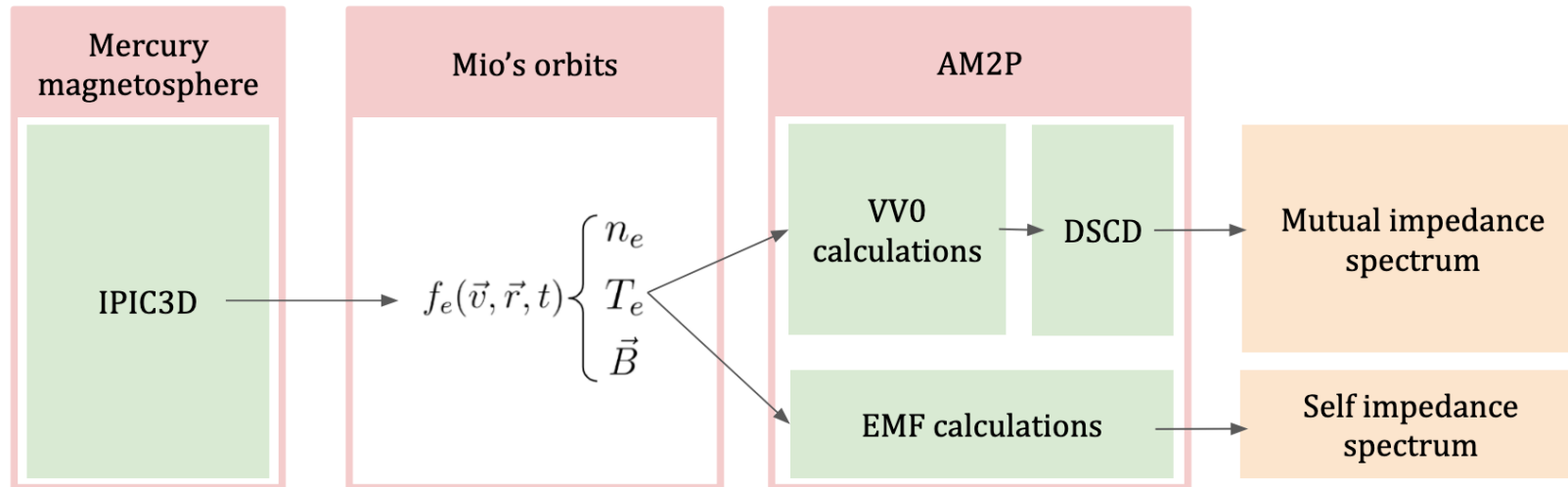


We take into account
the spacecraft influence
(with DSCD code)

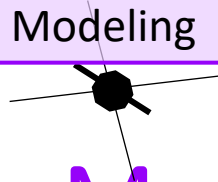
Instrumental Response Modeling of Mutual Impedance

→ Diagnostic of electron population:

currently working on simulations of the future data measured by BepiColombo:



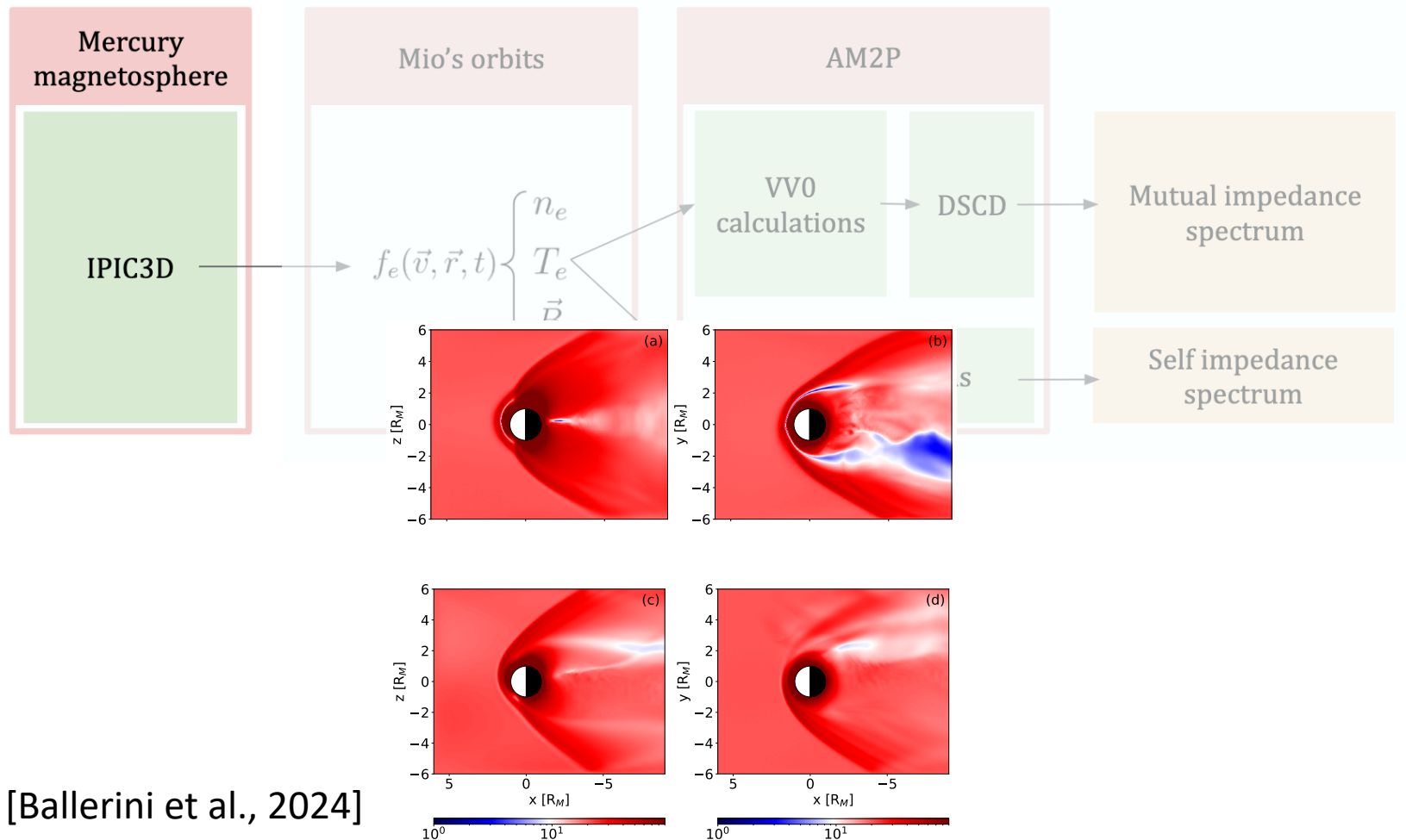
[Pallu et al., to be submitted in July]



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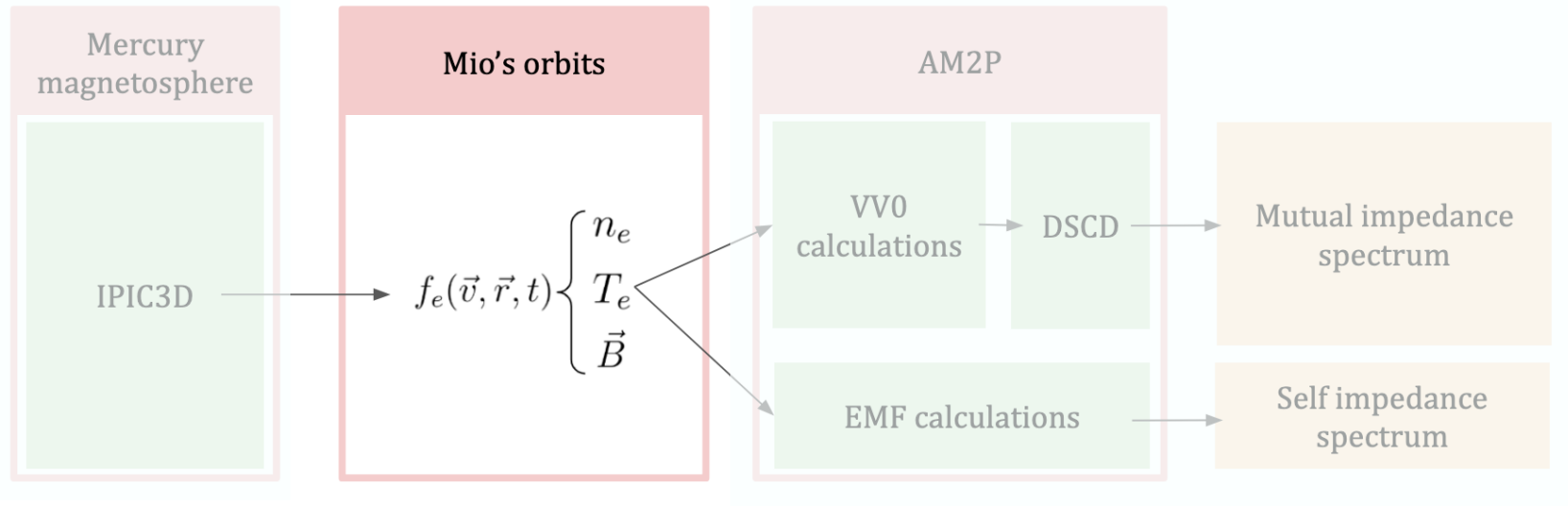


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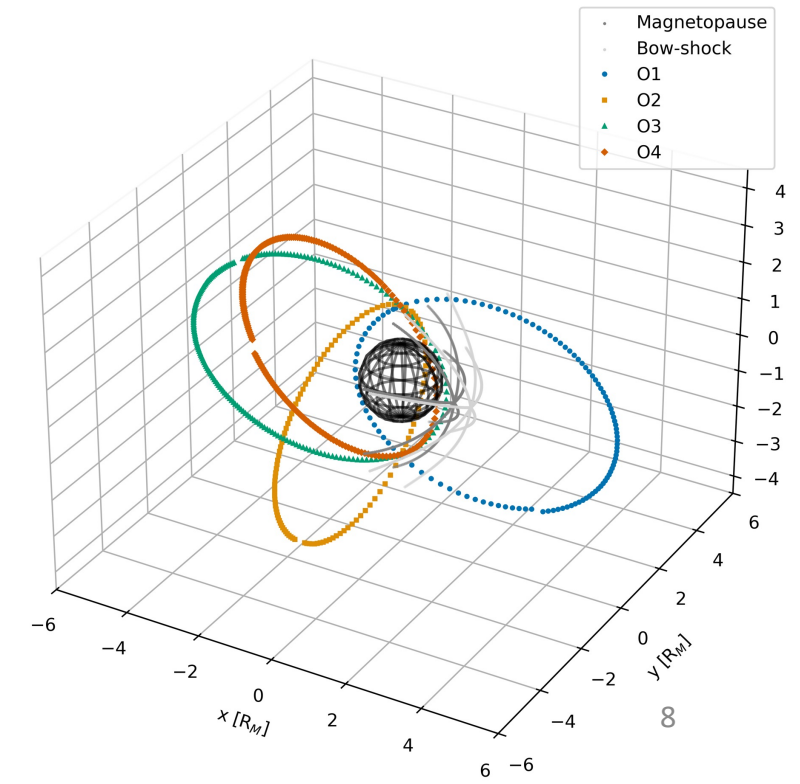
[Ballerini et al., 2024]

Instrumental Response Modeling of Mutual Impedance

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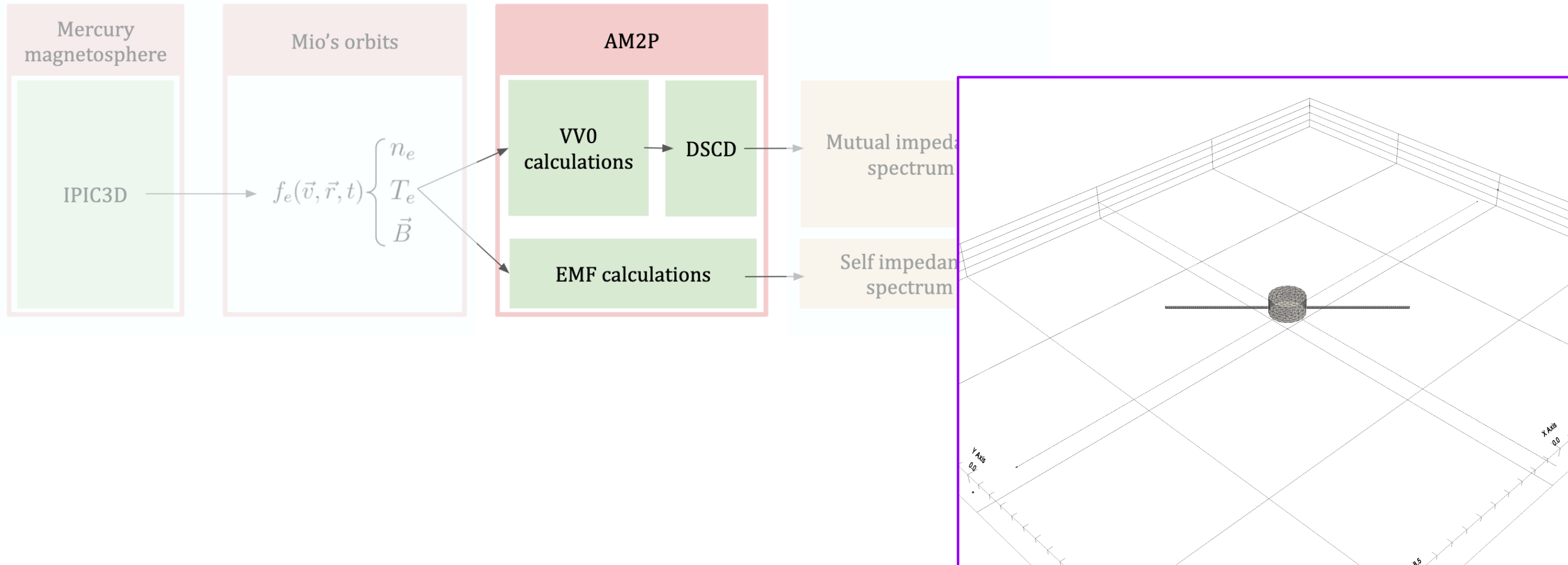


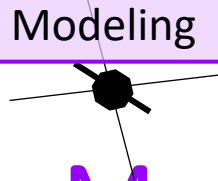
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Instrumental Response Modeling of Mutual Impedance

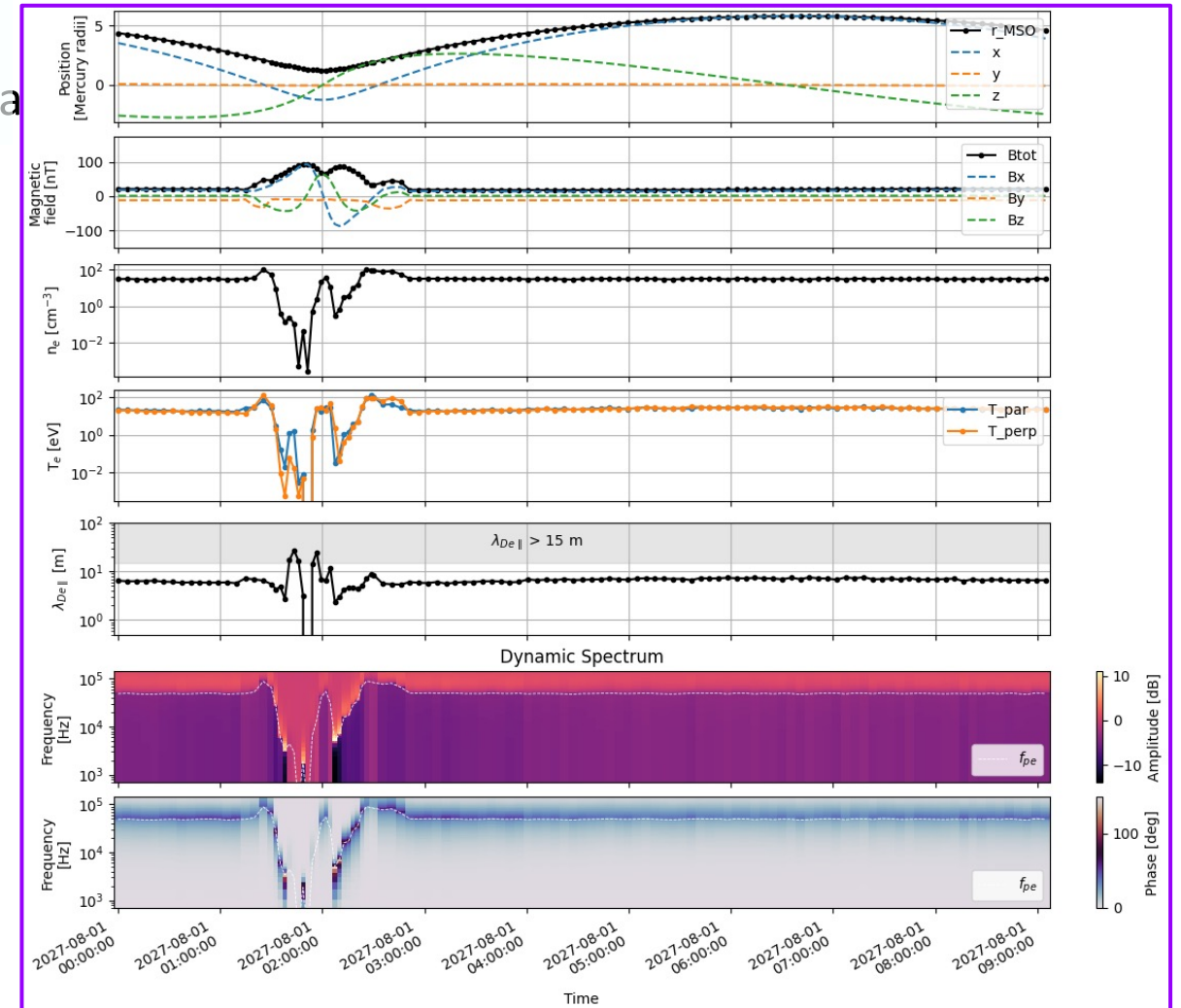
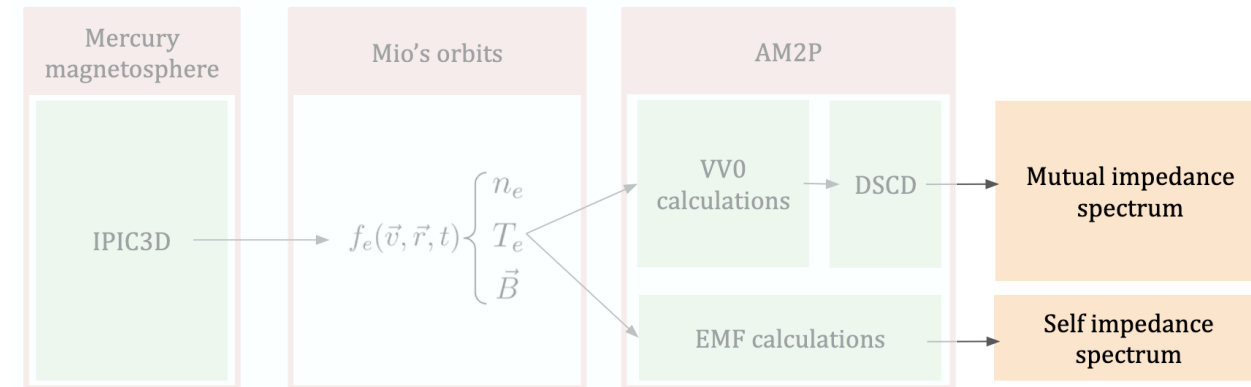
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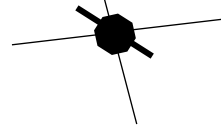


Instrumental Response Modeling of Mutual Impedance

→ Diagnostic of electron population:
currently working on simulations of the future data



[Pallu, Dazzi, Henri, Vallières, Ballerini, Carme, Elliott, et al., to be submitted in July]



Objectives

Prepare the BepiColombo future data

- Diagnostic of electron populations

But also:

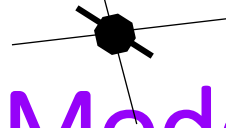
- Try to make a diagnostic of **ions** *in some configurations!*

Why?

- the response is dominated by electrons
- ions oscillate at lower frequencies
→ frequencies not in the instrumental frequency range

How:

We need to add the ion contribution in AM²P response model

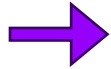


Instrumental Response Modeling

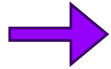
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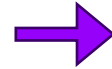
Vlasov +
Poisson
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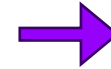
Linearisation
+ Fourier



Use Maxwellian
velocity
function



Calculate
dielectric
 $\varepsilon(k, \omega)$



Calculate the
wave potential
 V/V_0



Already modelised by a
fortran code
(written by N. Gilet)

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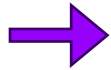


Instrumental Response Modeling

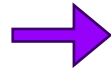
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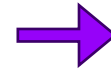
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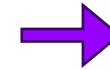
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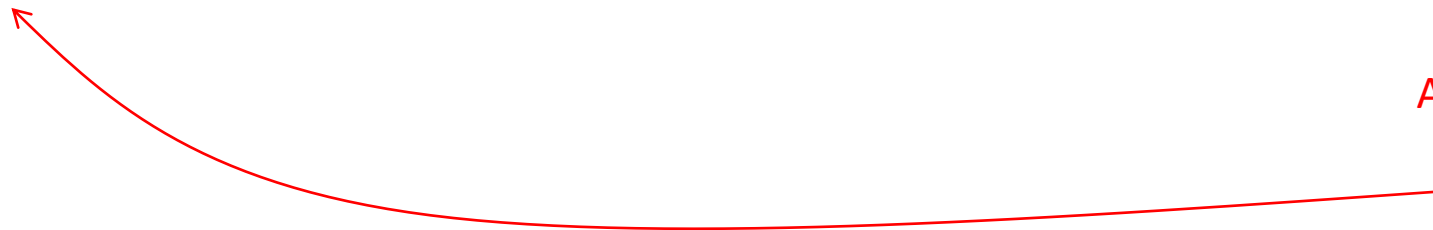


Already modelised by a
fortran code
(written by N. Gilet)

Also done for two **maxwellian**
distribution functions!

$$\begin{cases} \frac{\partial f}{\partial t}(\mathbf{x}, \mathbf{v}, t) + \mathbf{v} \cdot \nabla_{\mathbf{x}} f(\mathbf{x}, \mathbf{v}, t) + \frac{e}{m_e} \mathbf{E} \cdot \nabla_{\mathbf{v}} f(\mathbf{x}, \mathbf{v}, t) = 0 \\ \nabla \cdot \mathbf{E} = \frac{e}{\varepsilon_0} \int f(\mathbf{x}, \mathbf{v}, t) d\mathbf{v} \end{cases}$$

→ Vlasov eq. for **cold** electrons and **hot** electrons

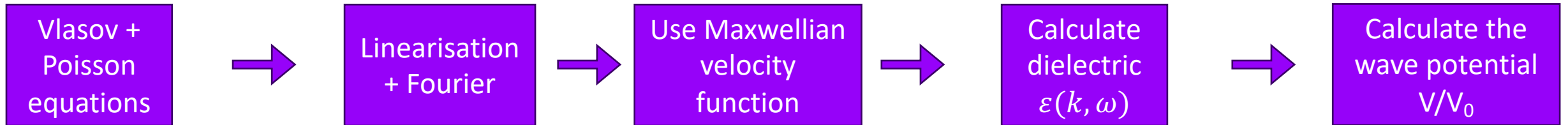




Instrumental Response Modeling **with ions**

We measure: $V_R(\omega)$
which depends on: $\varepsilon(k, \omega)$

We need to calculate $\varepsilon(k, \omega)$ theoretically:



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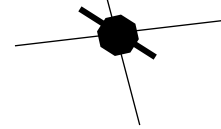
→ Vlasov eq. for **cold** electrons and **hot** electrons

→ Use this code and adapt it for 2 populations:

- one electron population
- one ion population

Already modelised by a
fortran code
(written by N. Gilet)

Also done for two **maxwellian**
distribution functions!

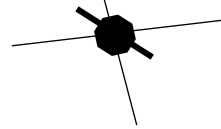


Comparison of cases

Electron maxwellian:

2 Electron maxwellian:

2 Electron/ion maxwellian:



Comparison of cases

2 Electron maxwellian:

2 Electron/ion maxwellian:

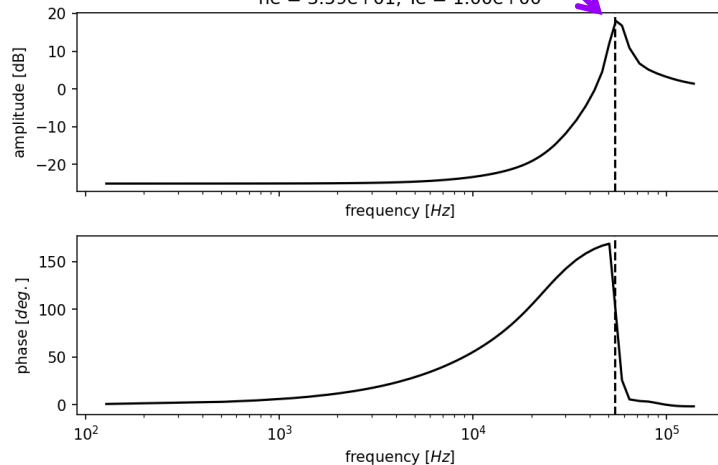
Electron maxwellian:

e^- population with (T_e, n_e)

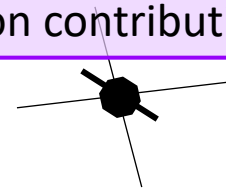


Only Langmuir waves and f_{pe} visible

PWI/AM2P unmagnetized Maxwellian plasma response
 $n_e = 3.59e+01, T_e = 1.00e+00$



Spectrum from modelisation



Comparison of cases

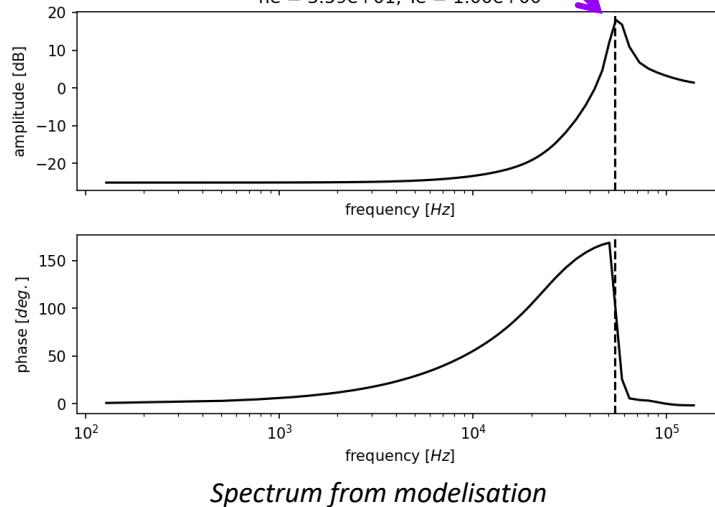
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Only Langmuir waves and f_{pe} visible

PWI/AM2P unmagnetized Maxwellian plasma response
 $n_e = 3.59e+01, T_e = 1.00e+00$



2 Electron maxwellian:

e_H population with (T_H, n_H)

e_C population with (T_C, n_C)

These parameters were used:

$$\mu = n_H/n_C$$

$$\tau = T_H/T_C$$



Necessary:
 $T_H \gg T_C$

2 waves:

Langmuir and electron acoustic waves

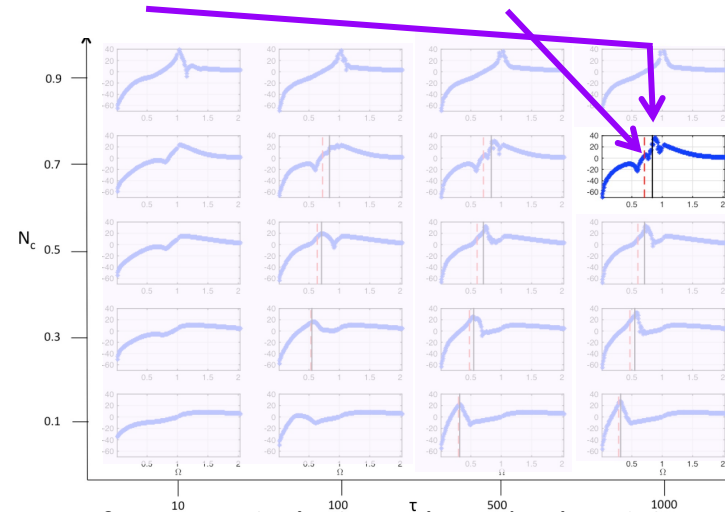
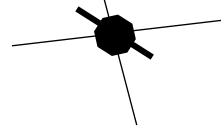


Fig. from N. Gilet's thesis (2019) – (modelisation)

2 Electron/ion maxwellian:



Comparison of cases

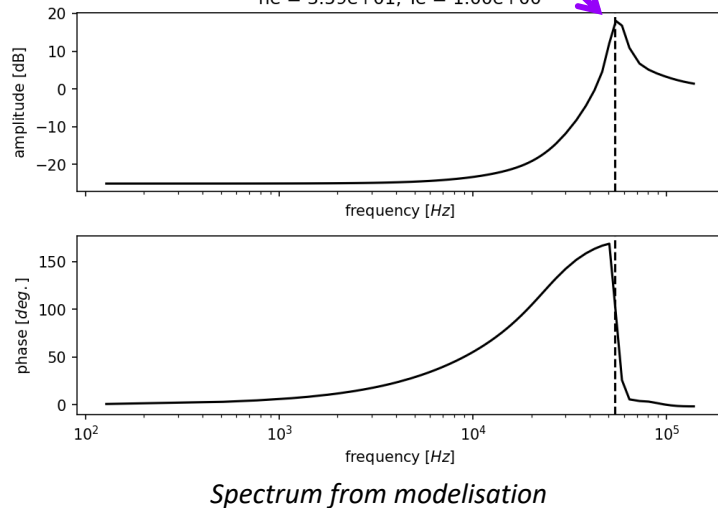
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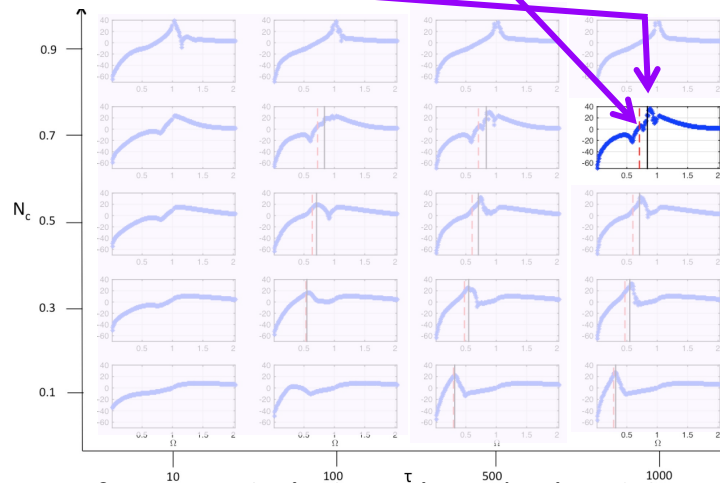


Fig. from N. Gilet's thesis (2019) – (modelisation)

2 Electron/ion maxwellian:

e^- population with (T_e, m_e)

ion population with (T_i, m_i)

We now use these parameters:

$$\mu = m_i/m_e$$

$$\tau = T_i/T_e$$

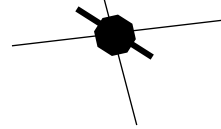


2 waves:

Langmuir and ion acoustic waves

$$\epsilon(k, \omega) = 1 - \frac{1}{k^2} Z'(X_{ie}) - \frac{1}{k^2} \frac{T_e}{T_i} Z'(X_{ii})$$

Necessary:
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Comparison of cases

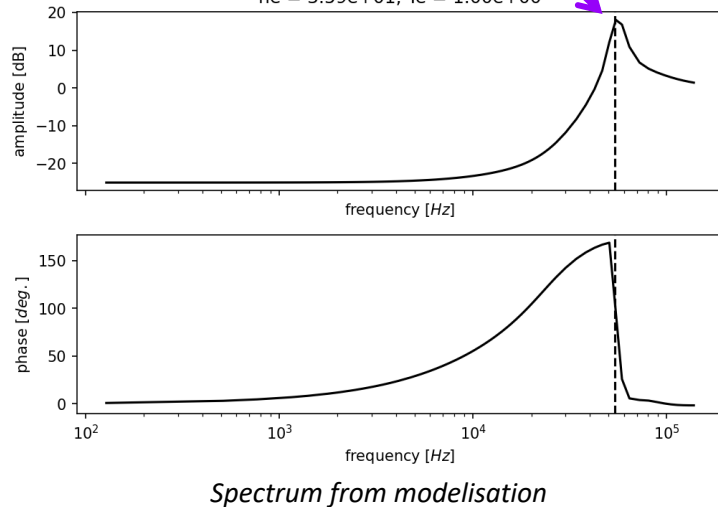
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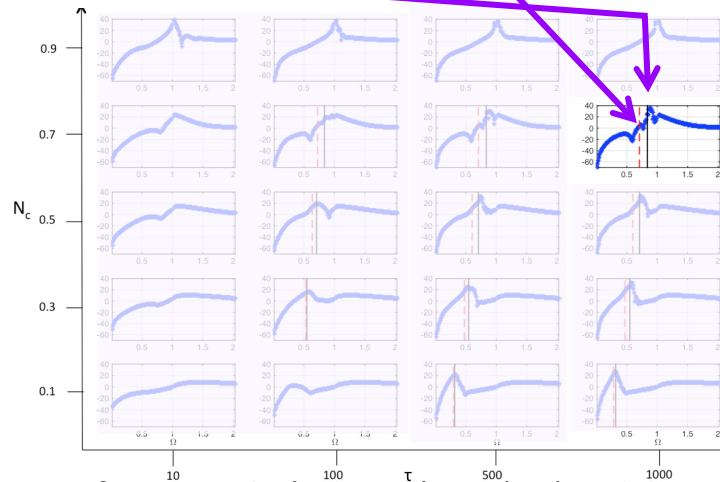


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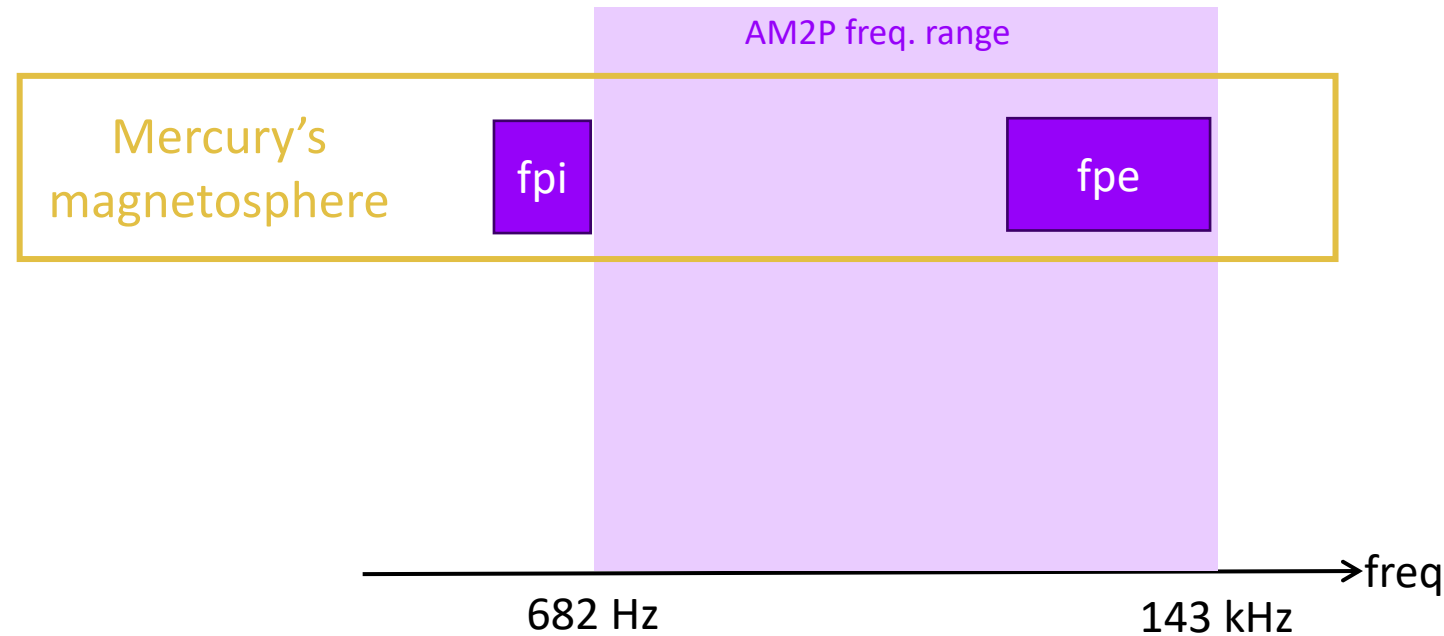
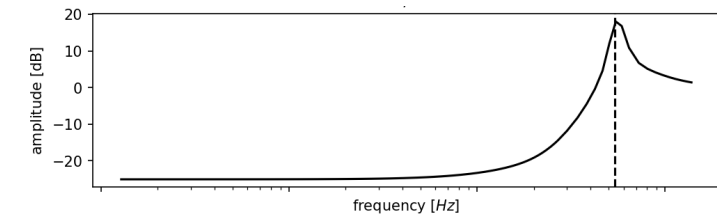
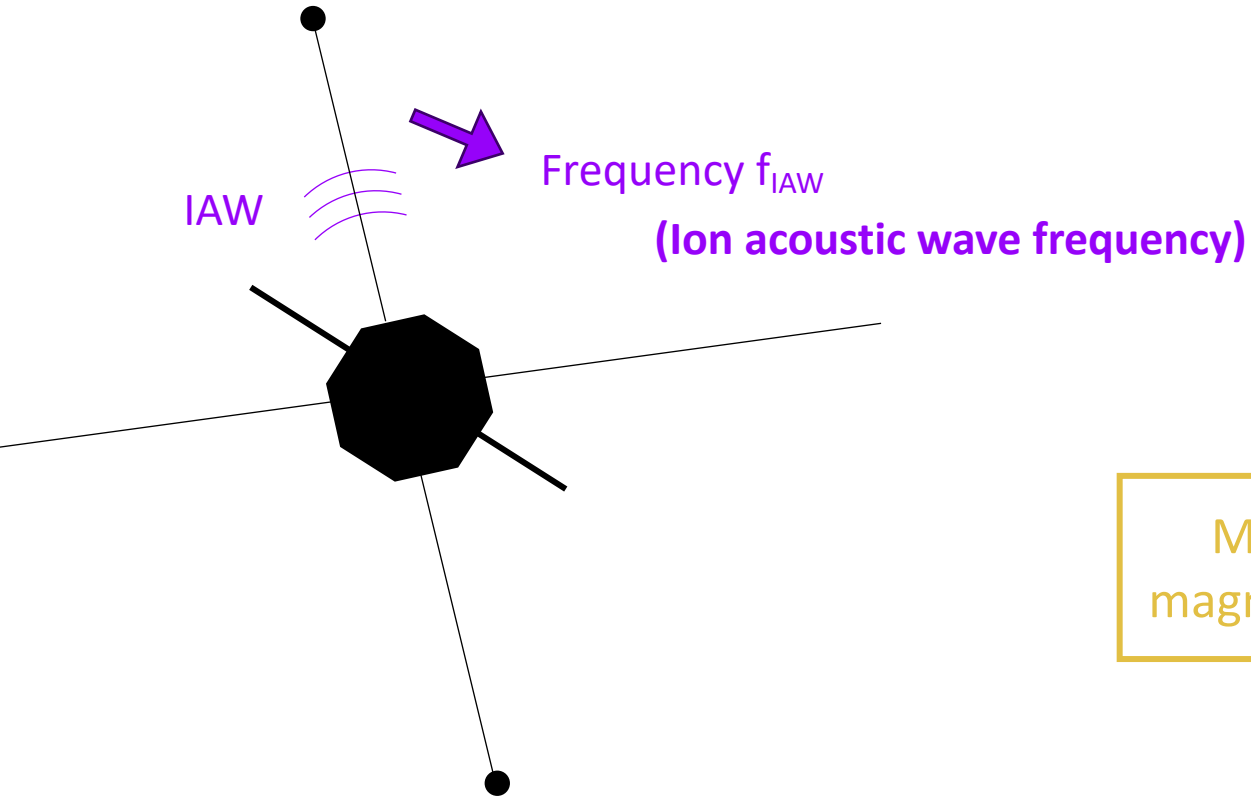
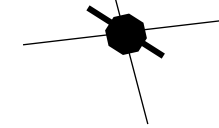
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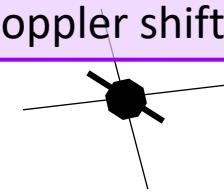
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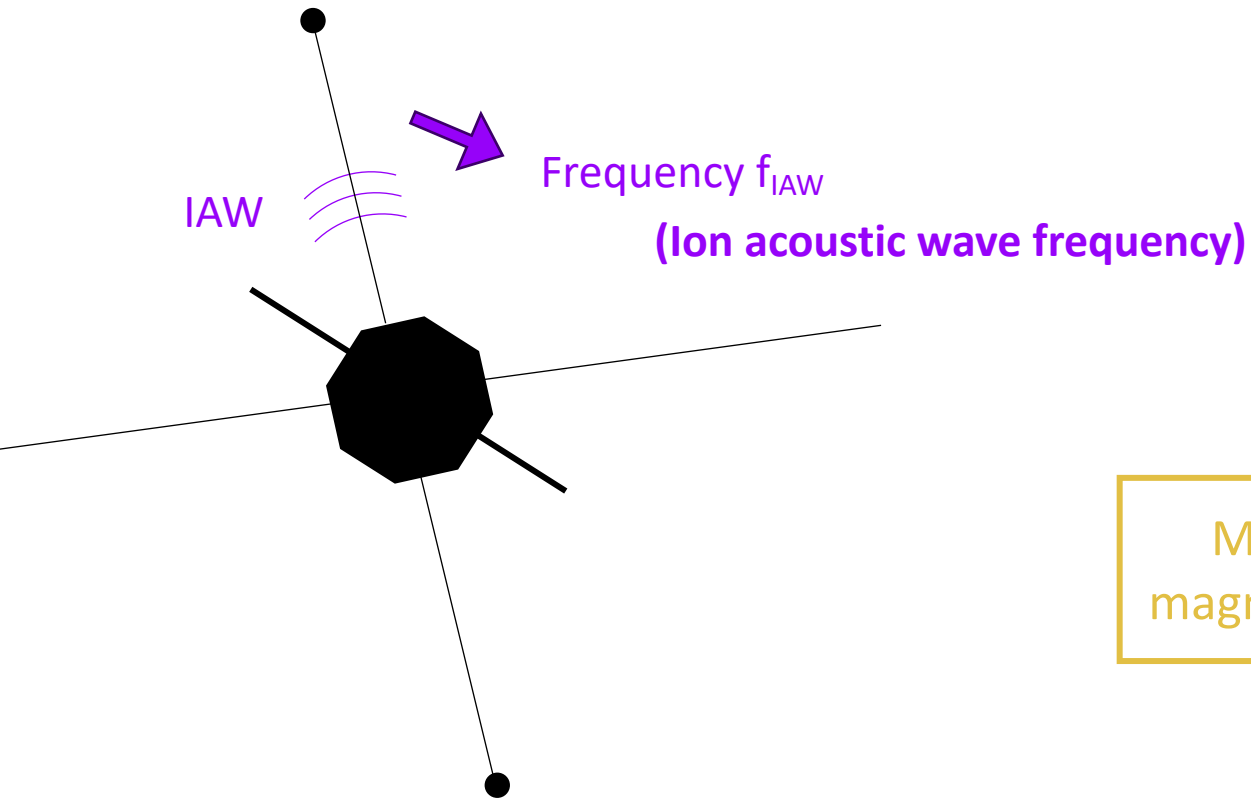
Necessary:
 $T_e \gg T_i$

→ Possible in the solar wind with BepiColombo



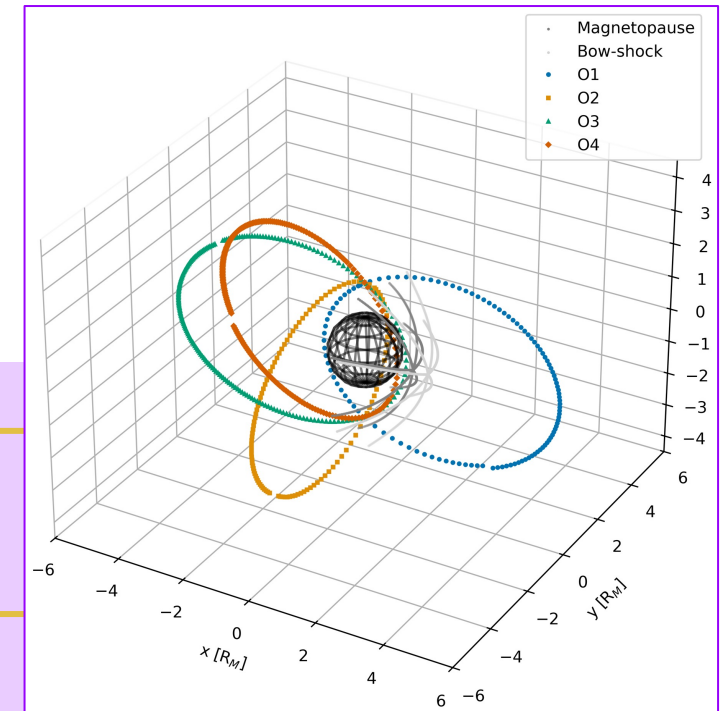


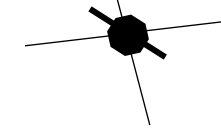
BepiColombo will go
in the solar wind
for a big part of its orbits:



Mercury's magnetosphere

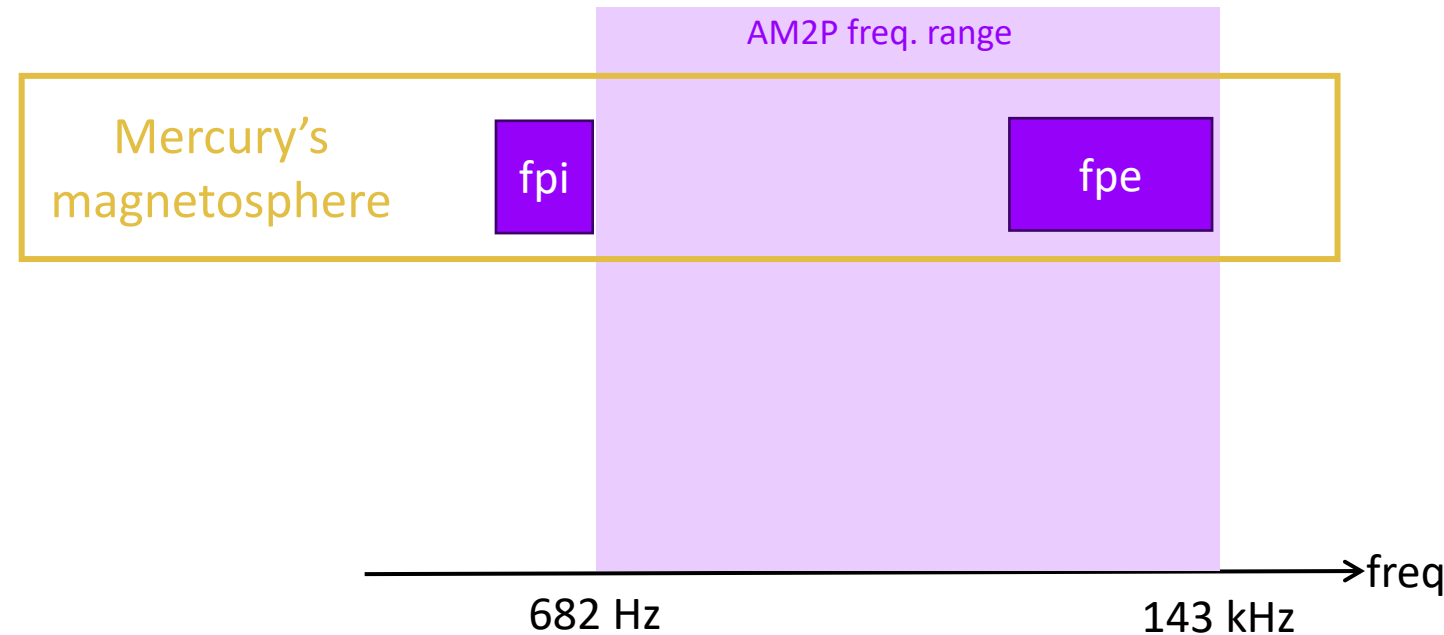
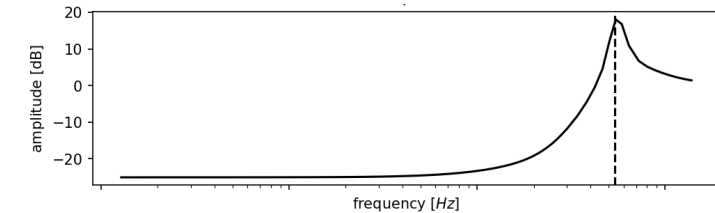
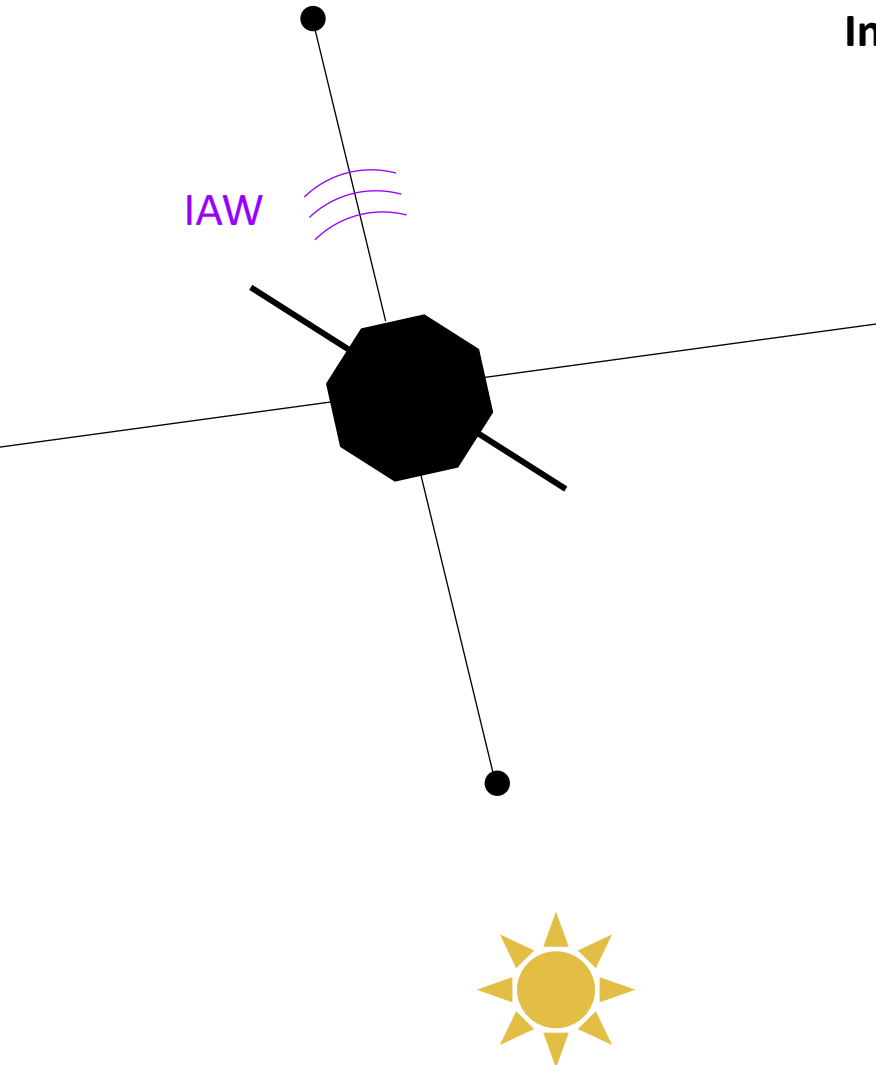
fpi

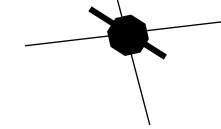




The power of the Doppler shift

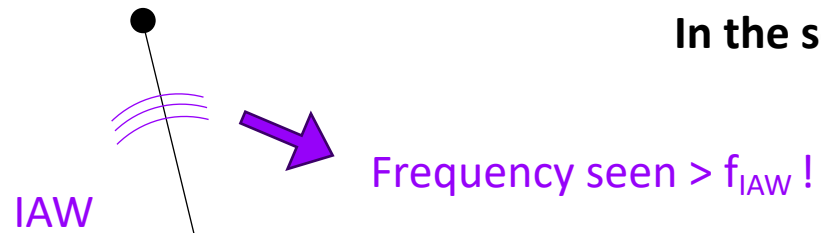
In the solar wind:





The power of the Doppler shift

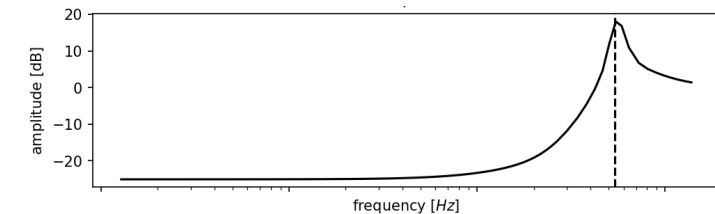
In the solar wind:



Frequency seen $> f_{IAW}$!

The spacecraft appears to be stationary, but the plasma is flowing with the solar wind:

$$\omega \rightarrow \omega' = \omega - \vec{k} \cdot \vec{v}_{SW}$$



Mercury's magnetosphere

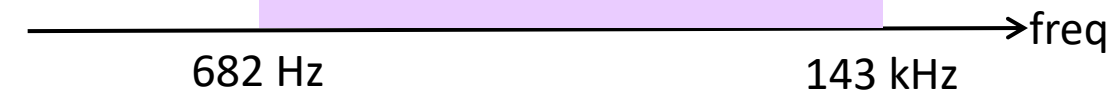
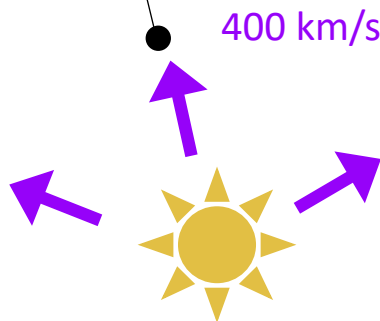
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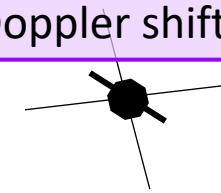
AM2P freq. range

fpe

400 km/s

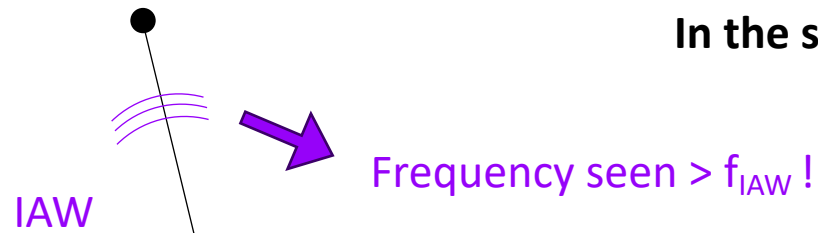
Solar wind





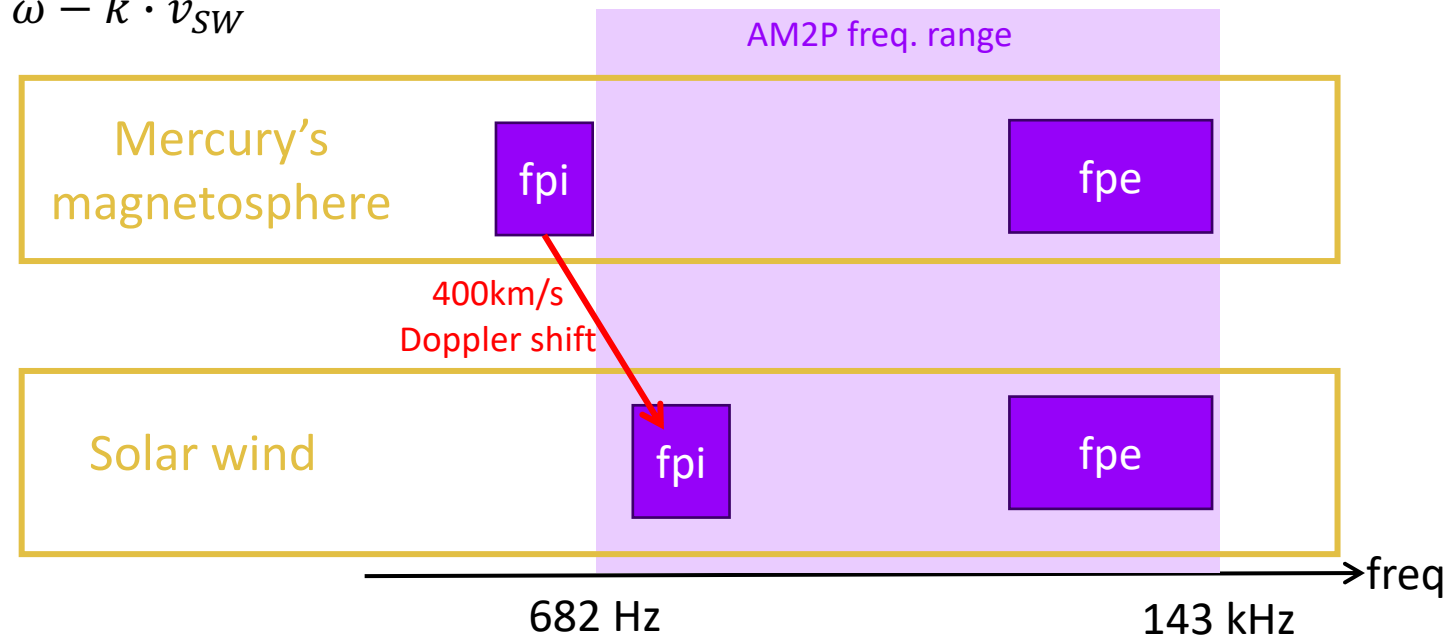
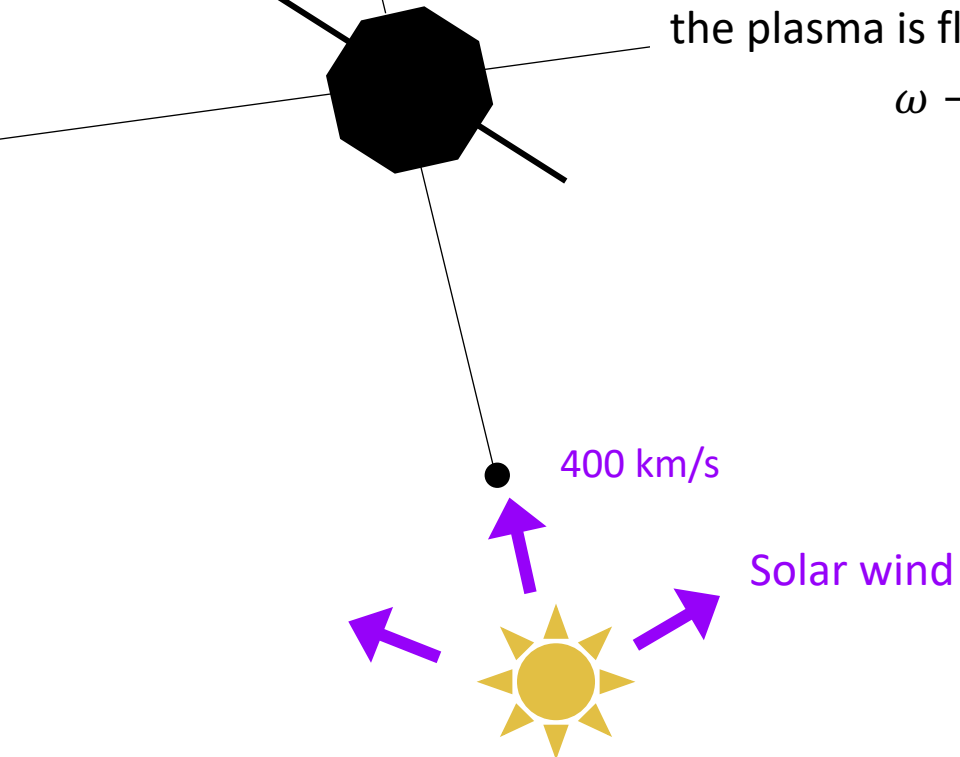
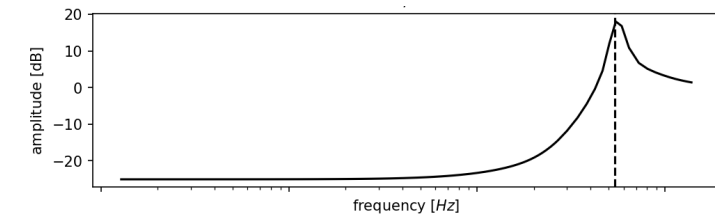
The power of the Doppler shift

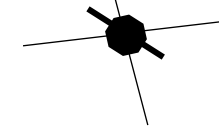
In the solar wind:



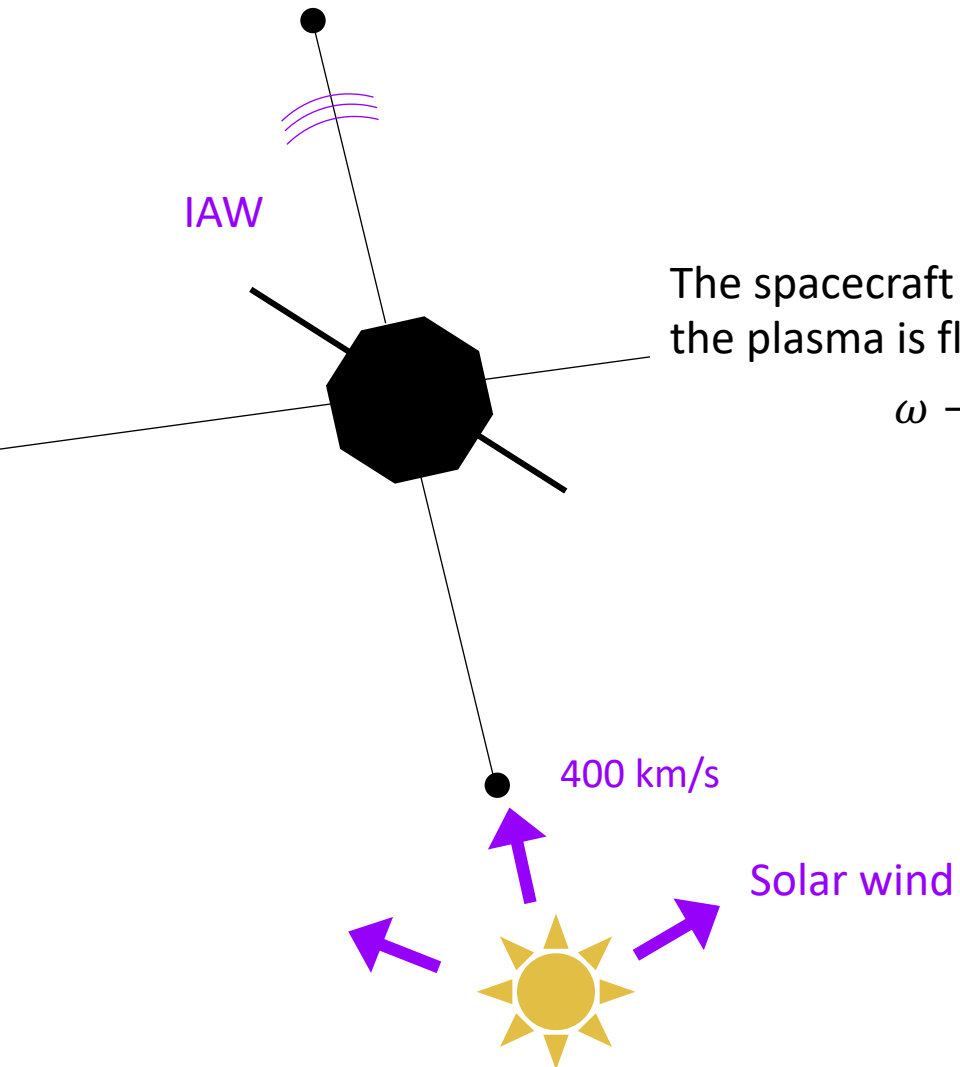
The spacecraft appears to be stationary, but the plasma is flowing with the solar wind:

$$\omega \rightarrow \omega' = \omega - \vec{k} \cdot \vec{v}_{SW}$$



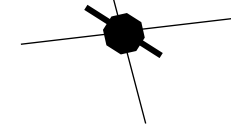


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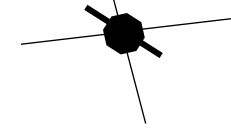
→ Particular configurations that should be tested:

- $\vec{k}$ and $\vec{v}_{SW}$ in the same direction
- $\vec{k}$ and $\vec{v}_{SW}$ in the opposite direction
- $\vec{k}$ perpendicular to $\vec{v}_{SW}$



Preliminary results

- Calculation of the dielectric ε
for IAW without solar wind drift



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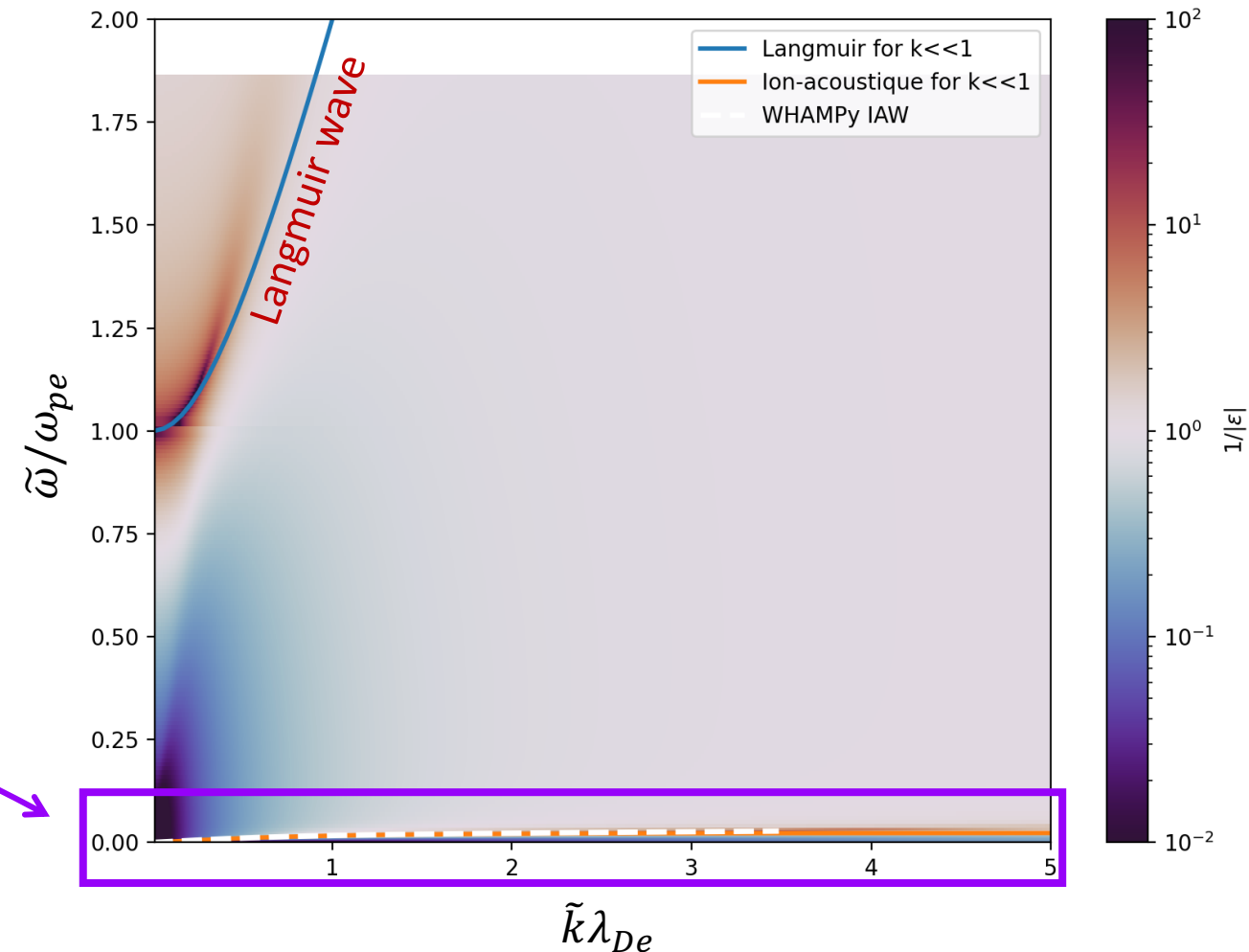
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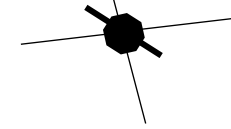
The color map shows:

$1/|\varepsilon|$ as a function of normalized wavenumber $\tilde{k}\lambda_{De}$ and normalized frequency $\tilde{\omega}/\omega_{pe}$

Red peaks = plasma normal modes,
i.e. solutions of the dispersion relation $\varepsilon(\tilde{k}, \tilde{\omega}) = 0$

Ion acoustic wave dispersion relation
is located here





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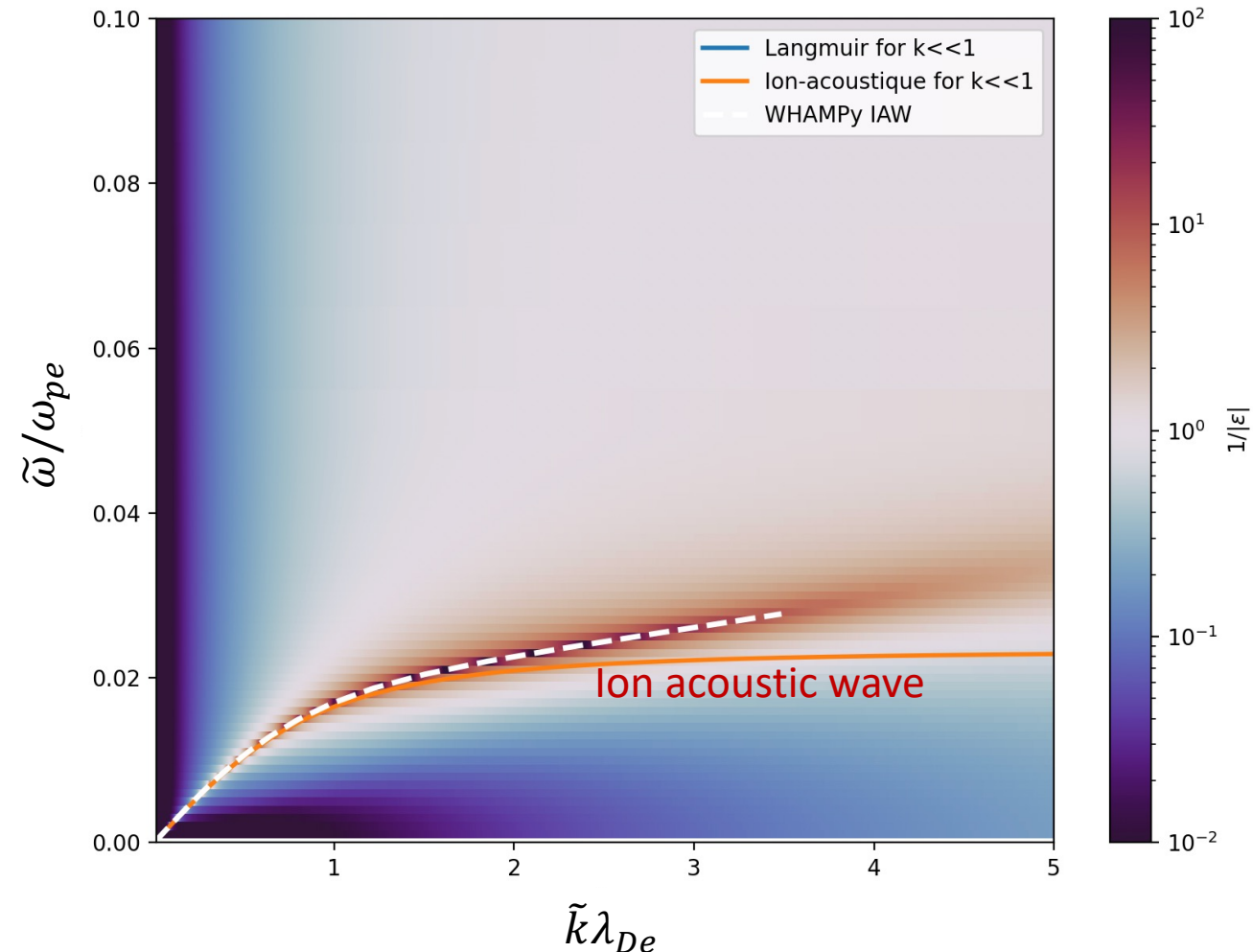
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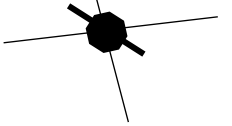
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→ Great agreement between:

- our calculations
- theory for $k \ll 1$
- simulation results from Whamp

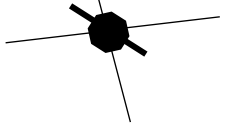
(Zoom)





Conclusions:

- We have used a global kinetic simulation of mercury magnetosphere to produce synthetic spectra that should be measured by BepiColombo/AM²P
- BepiColombo offers this unique opportunity to get ion measurements with mutual impedance experiment
- We need to extend the current instrumental model in order to better predict the signal that we will measure

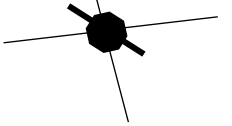


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+ more precise objectives :

- Determine in which conditions these ions are visible in AM2P data
- Understand which signature they produce in a spectrum
- Evaluate which ion parameters could be constrained (T_i , ?)



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Thank you!