

Modeling of mutual impedance experiments and quasi-thermal noise spectroscopy in magnetized plasma

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Introduction: electron in situ measurements

Passive:



Active:



Collection of particles:

Electrostatic analyzer,
Faraday cup

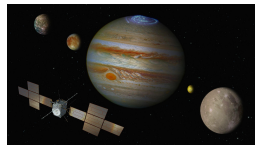
Langmuir probe

Collective behaviors,
coupling with fields:

Quasi-thermal noise spectroscopy

Mutual impedance, relaxation sounders

JUICE,
ESA



RPWI-MIME



Jupiter



Ganymede

Mio-BepiColombo,
ESA-JAXA



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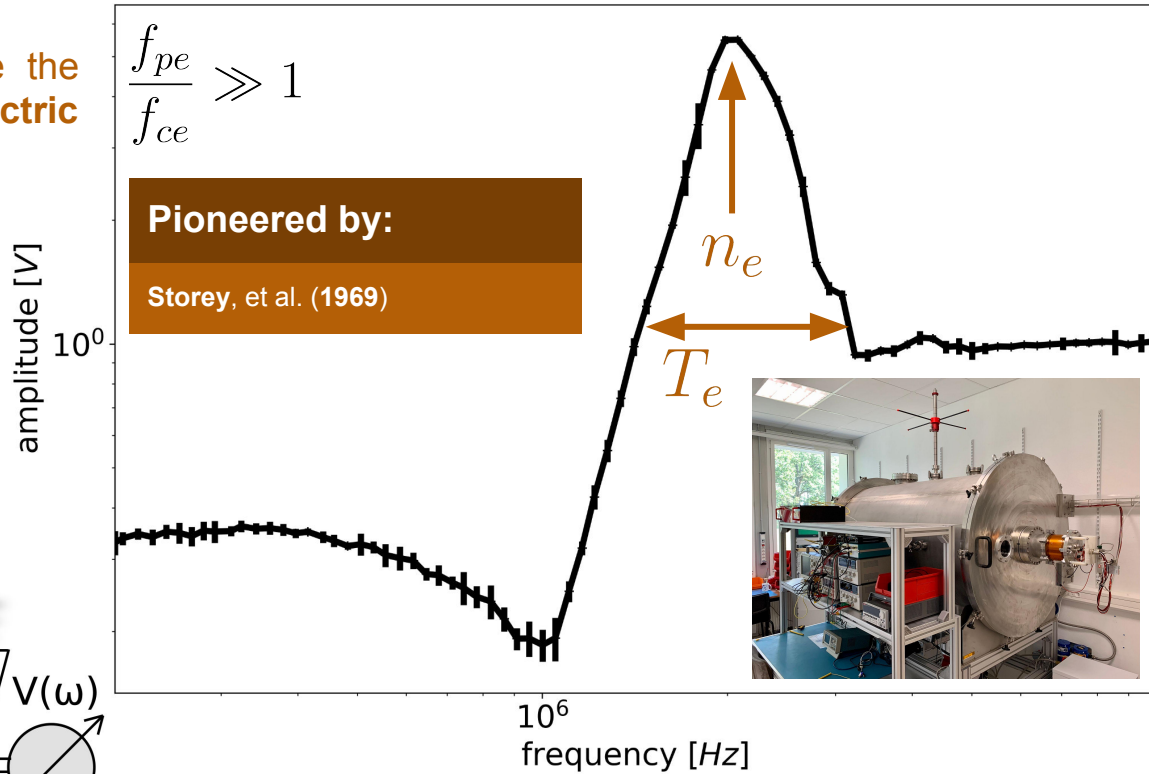
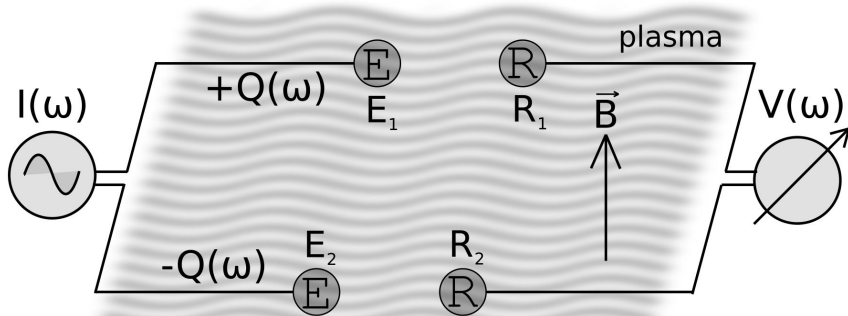


Mercury

Mutual impedance - definition

Mutual impedance experiments measure the **mutual impedance** between a **pair of electric antennas** embedded in the plasma.

$$Z(\omega) = \frac{V(\omega)}{I(\omega)}$$



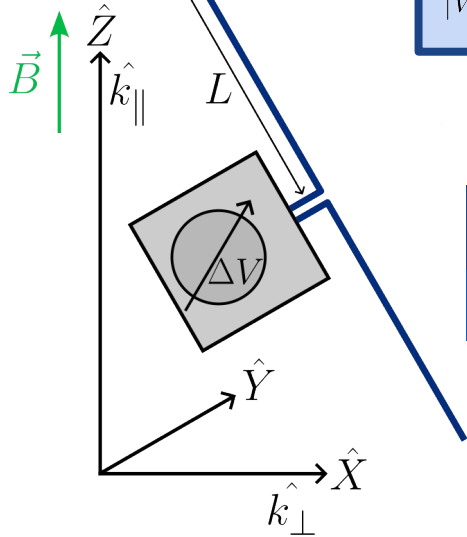
Typical mutual impedance spectrum, measured in the PEPISO plasma chamber at LPC2E (Orleans, FR), obtained by compensating for the Earth magnetic field.

Quasi-thermal noise - definition

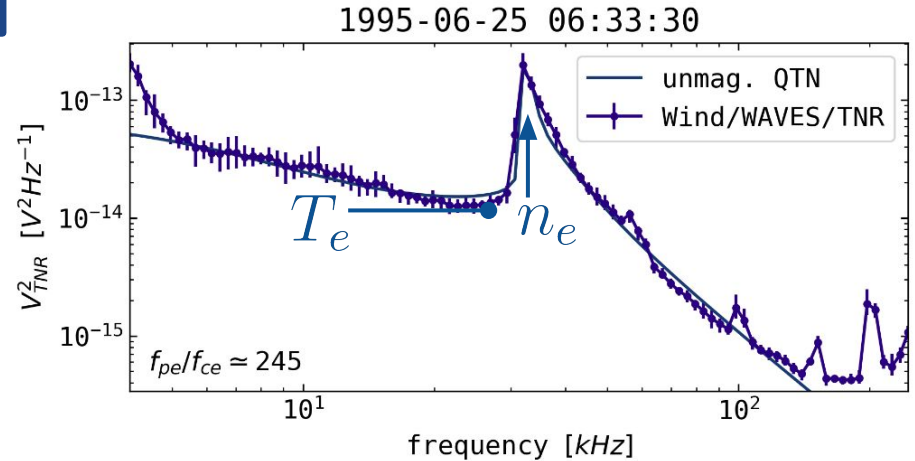
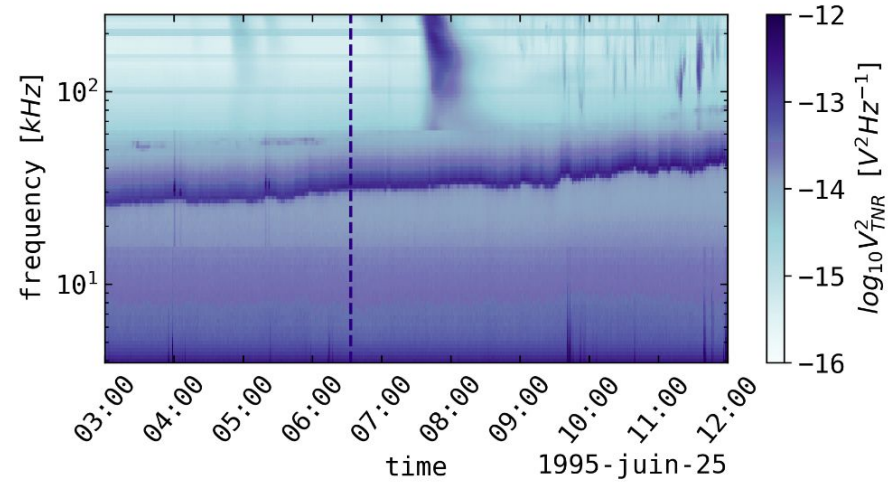
Quasi-thermal noise spectroscopy measures the **power spectrum of the potential difference** between the terminals of an electric antenna embedded in the plasma.

$$P_a = \int \mathbf{E}(\mathbf{r}, t) \cdot \mathbf{J}_a(\mathbf{r}) d^3r = V_0(t) I_a$$

$$|V_0(\omega)|^2 = \int \langle V_0(t_1) V_0(t_1 + t) \rangle e^{i\omega t} dt$$



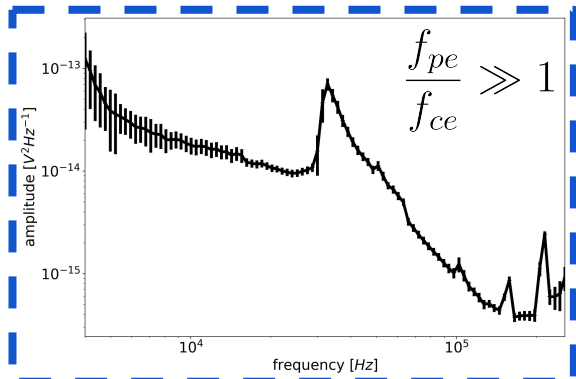
Pioneered by:
Meyer-Vernet, et al. (1979)



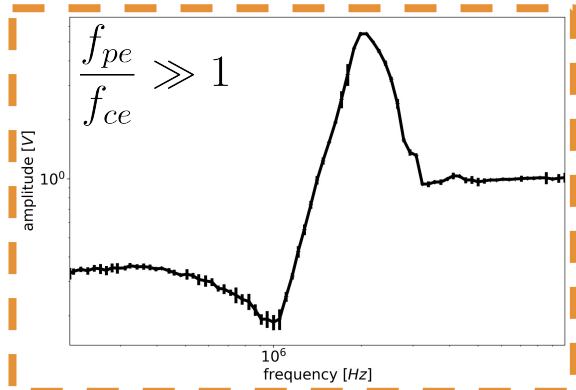
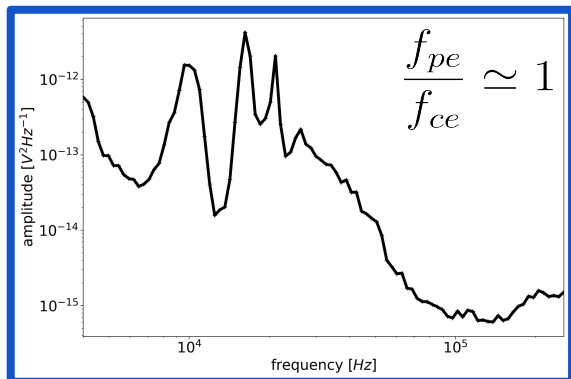
Representative example of quasi-thermal noise spectrum for a wire dipole antenna, measured by the WIND/TNR receiver on 25/06/1995 at 06:33 and averaged over one minute.

Limits and scope

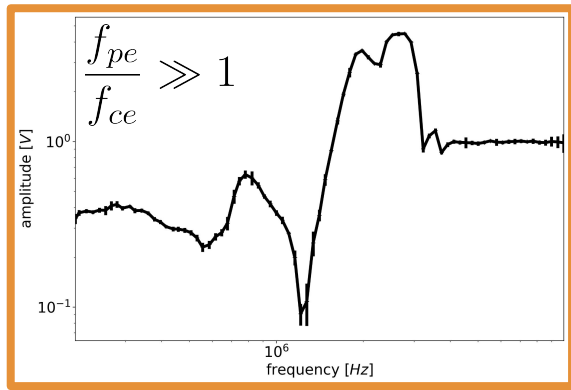
The **mutual impedance** and **quasi-thermal noise** spectra differ in the unmagnetized and magnetized case, crucially in the presence of additional local maxima.



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Magnetized mutual impedance model

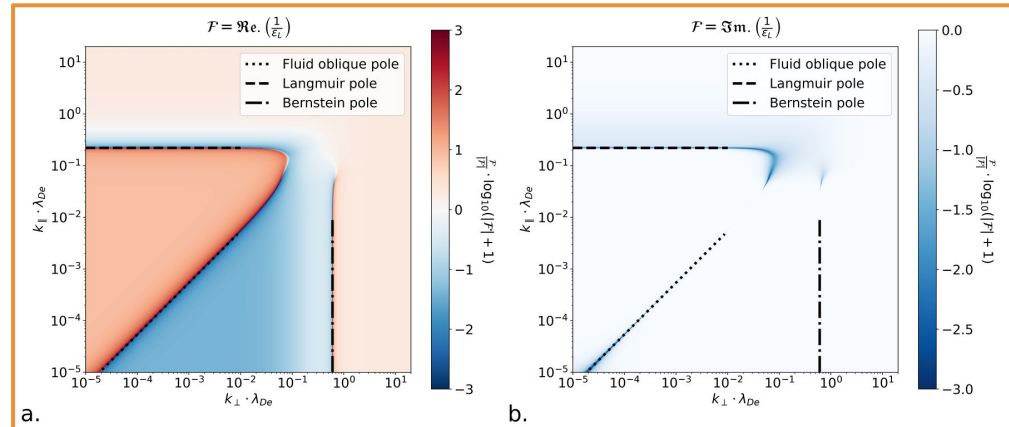
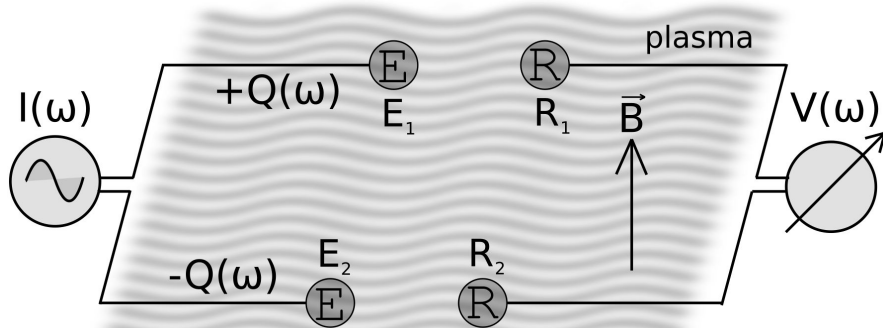
The model is based on the computation of the **electric potential** generated by the electric point charge deposited on the emitter antenna.

Hypothesis:

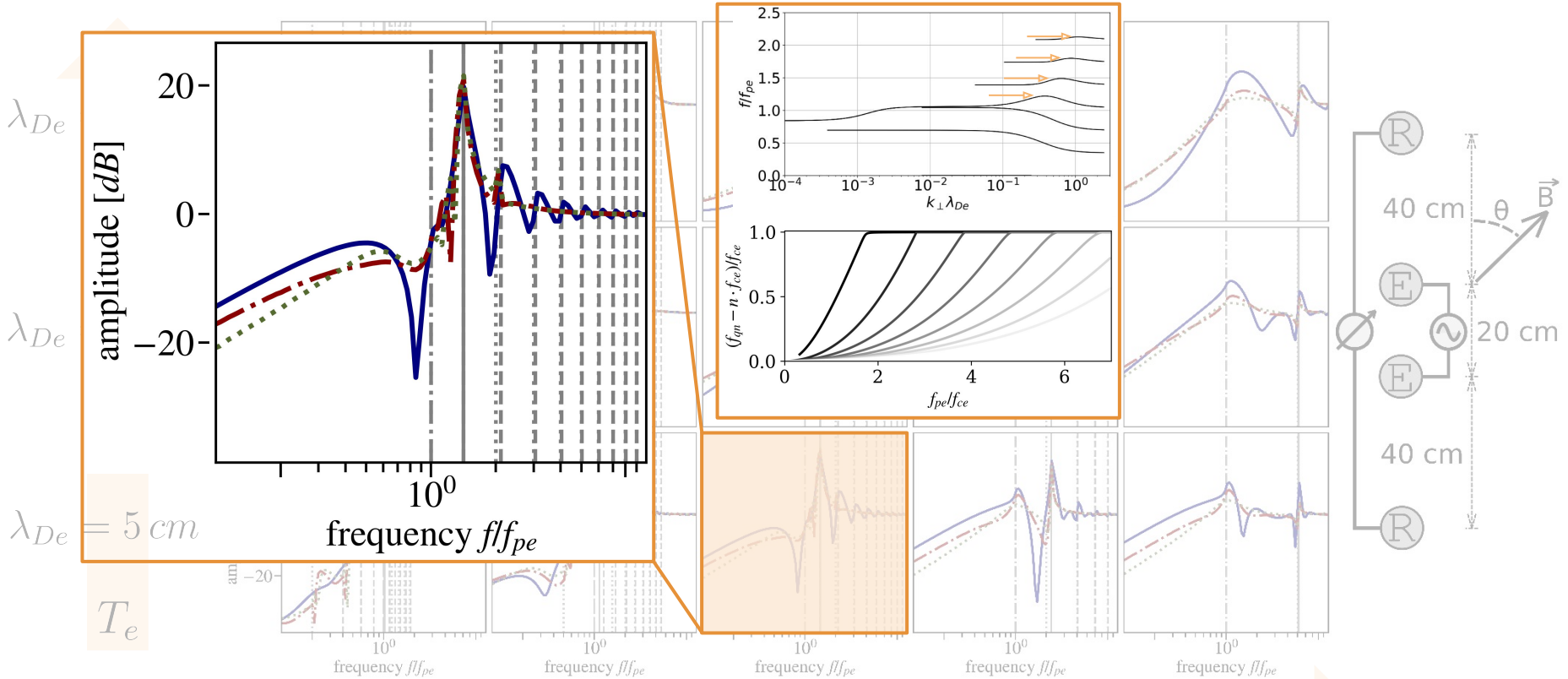
- Kinetic (Vlasov) model,
- electrostatic approximation,
- linear dielectric.

$$\frac{f_{pe}}{f_{ce}} \simeq 1 \quad \longrightarrow \quad \frac{V}{V_0} = \frac{\sqrt{r^2 + z^2}}{\pi} \int_0^{+\infty} dk_r \int_0^{+\infty} dk_z \frac{k_r J_0(k_r r) \cos(k_z z)}{k^2 \varepsilon_L(k_r, k_z, \omega)}$$

Expression valid for:
isotropic Maxwellian,
anisotropic Maxwellian,
Maxwellian with weak
electron-neutral scattering.



Magnetized mutual impedance results

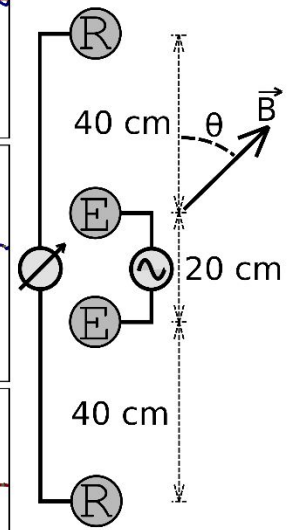
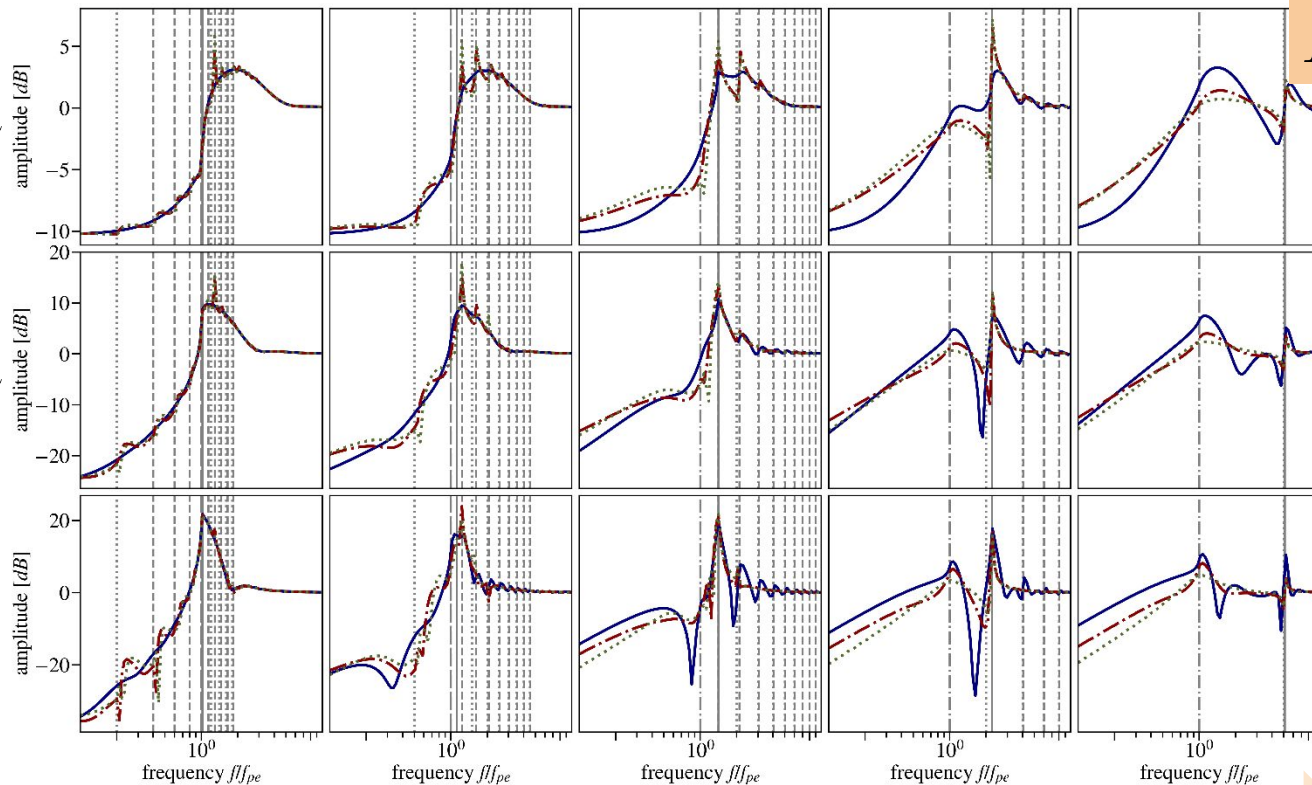


B $f_{pe}/f_{ce} = 5.0$ $f_{pe}/f_{ce} = 2.0$ $f_{pe}/f_{ce} = 1.0$ $f_{pe}/f_{ce} = 0.5$ $f_{pe}/f_{ce} = 0.2$

Magnetized mutual impedance results

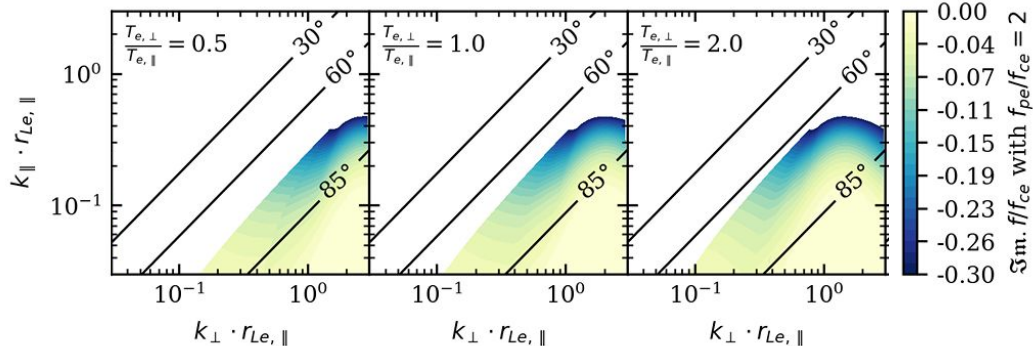
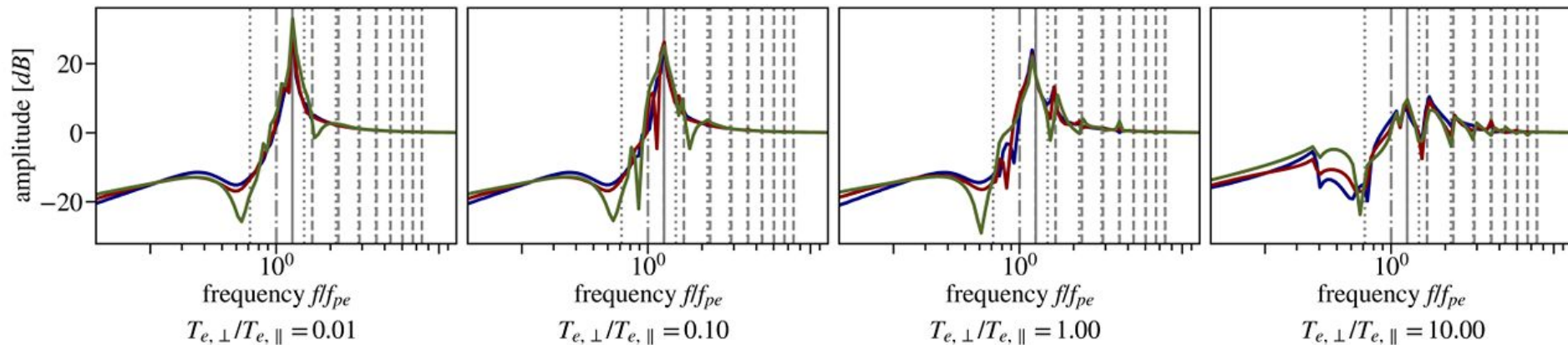
T_e electron temperature
 n_e plasma density
 B magnetic field

$\lambda_{De} = 20\text{ cm}$
 $\lambda_{De} = 10\text{ cm}$
 $\lambda_{De} = 5\text{ cm}$
 T_e



B $f_{pe}/f_{ce} = 5.0$ $f_{pe}/f_{ce} = 2.0$ $f_{pe}/f_{ce} = 1.0$ $f_{pe}/f_{ce} = 0.5$ $f_{pe}/f_{ce} = 0.2$

Magnetized mutual impedance results



- f_{qn}
- - - f_{pe}
- f_{uh}
- $\theta = 16.7 \text{ deg.}$
- $\theta = 45.0 \text{ deg.}$
- $\theta = 73.3 \text{ deg.}$

$T_{e,\perp}/T_{e,\parallel}$ electron temperature anisotropy

Magnetized quasi-thermal noise model

The model is based on the computation of the **fluctuations of the electric field** inside a plasma, as measured by quasi-thermal noise spectroscopy.

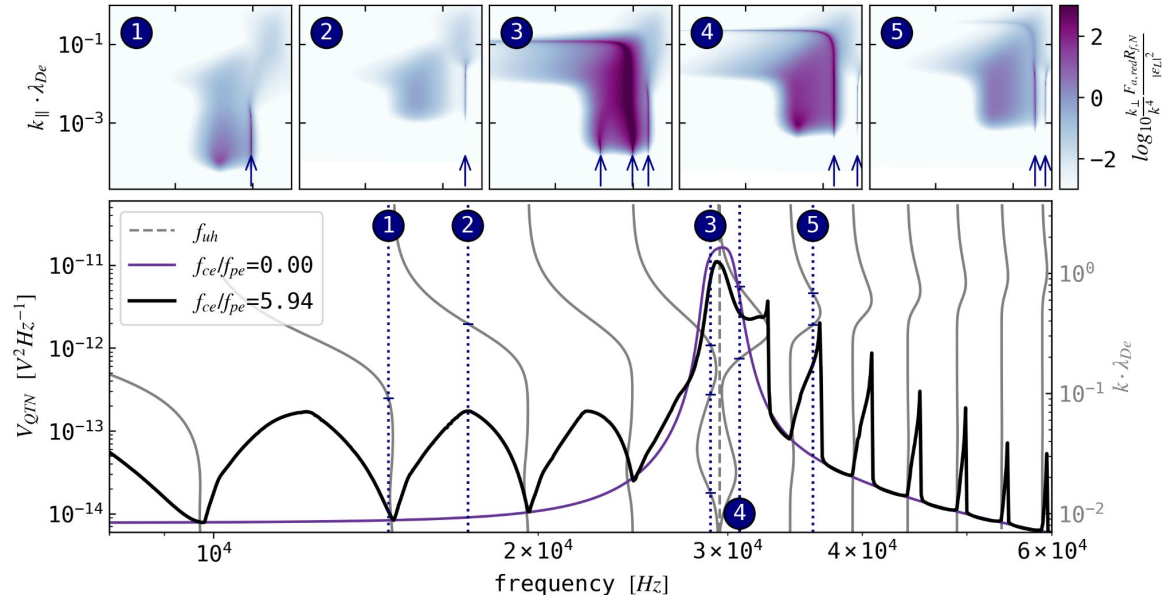
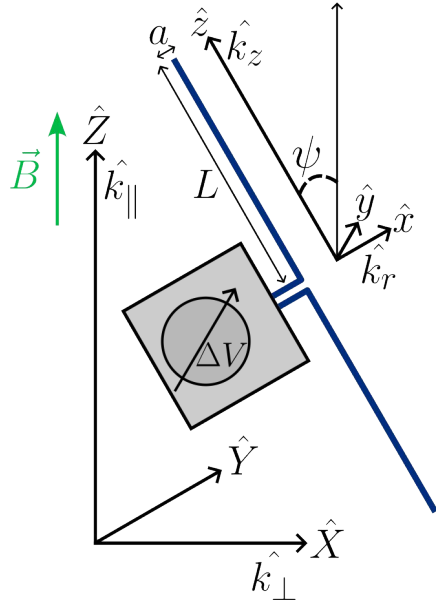
Hypothesis:

- Kinetic (Vlasov) model,
- electrostatic approximation,
- linear dielectric.

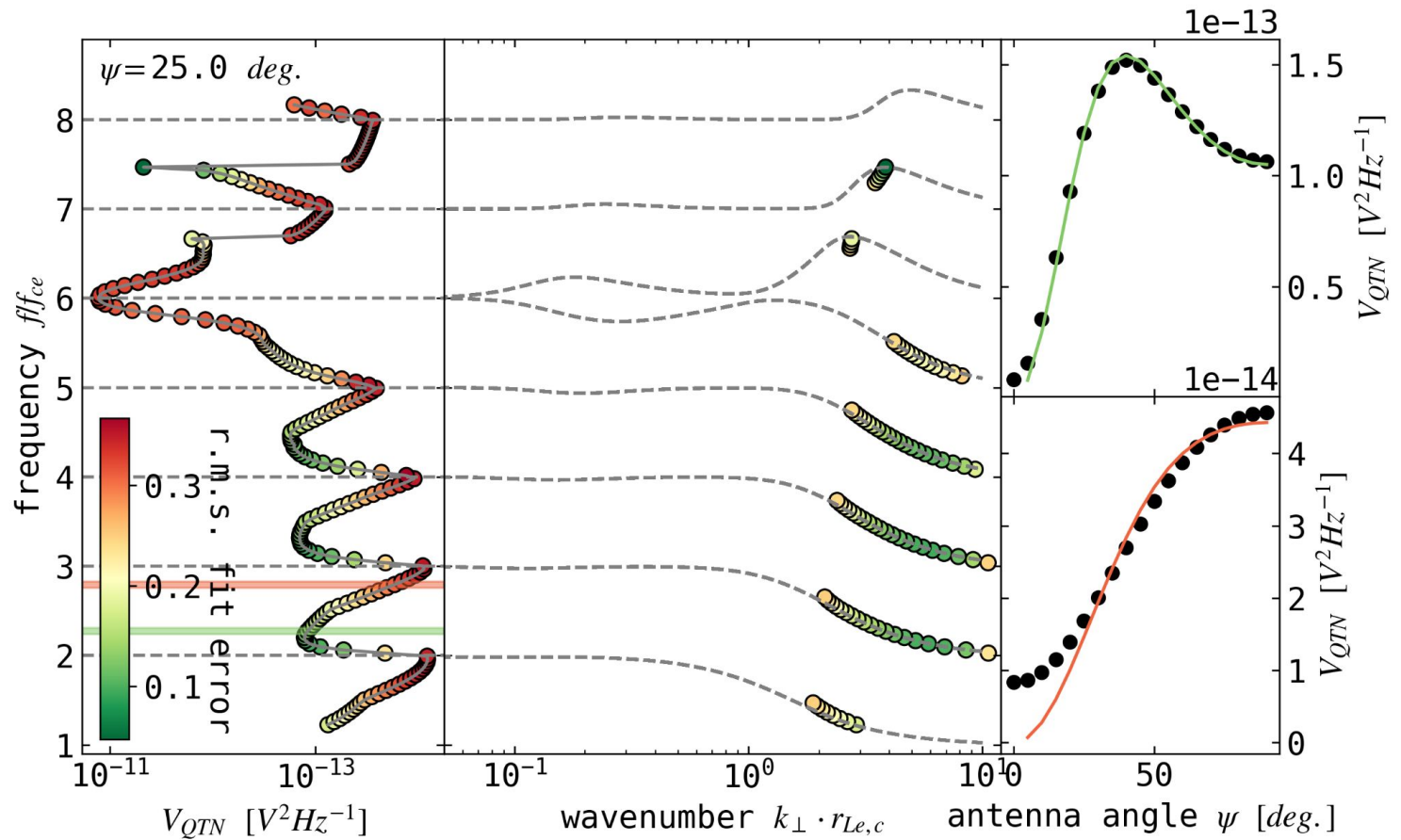
$$\frac{f_{pe}}{f_{ce}} \simeq 1$$

$$\longrightarrow |V_{QTN}(\omega)|^2 = C_i \int_0^{+\infty} \int_0^{+\infty} \frac{k_{\perp}}{k^4} \frac{F_{a,red} R_{f,N}}{|\varepsilon_L|^2} dk_{\parallel} dk_{\perp}$$

Expression valid for:
isotropic Maxwellian,
anisotropic Maxwellian,
Maxwellian with weak
electron-neutral scattering.

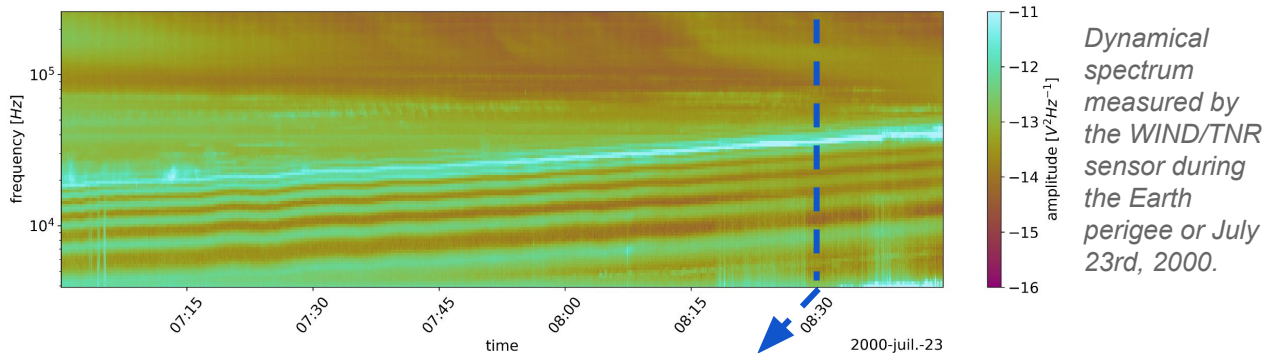


Magnetized quasi-thermal noise results

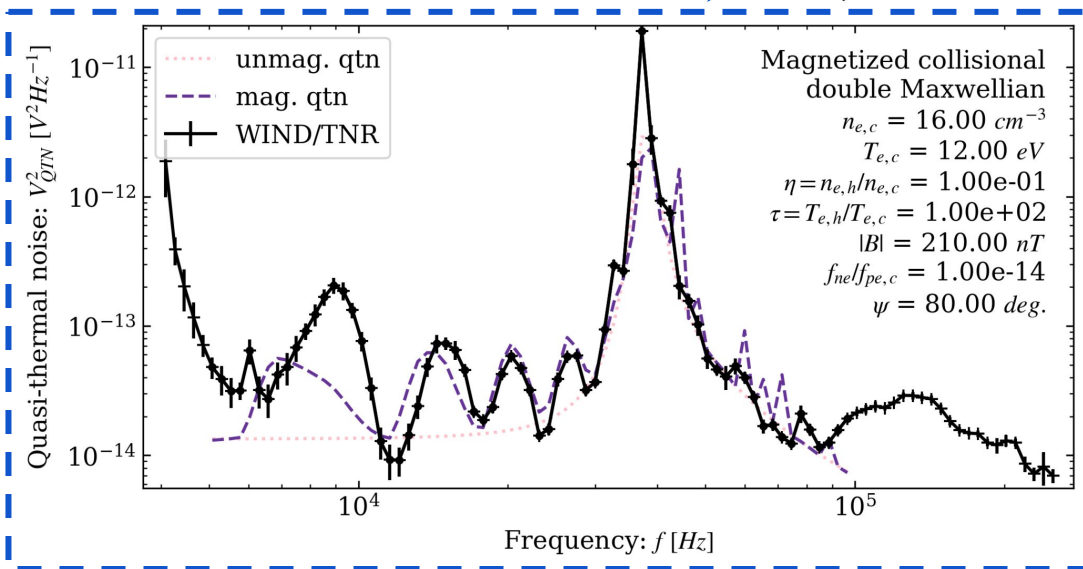
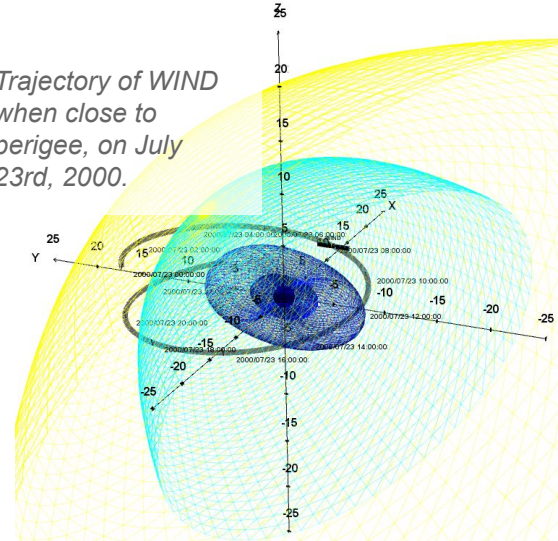


The magnetized quasi-thermal noise depends upon the angle between the antenna and the magnetic field. This dependency was investigated in (Moncuquet et al., 1995) by using measurements of the Ulysses/URAP receiver. We use the same approach to validate our numerical calculation.

Magnetized quasi-thermal noise results



Trajectory of WIND when close to perigee, on July 23rd, 2000.



Comparison between the spectrum measured by the WIND/TNR sensor and the magnetized quasi-thermal noise model.

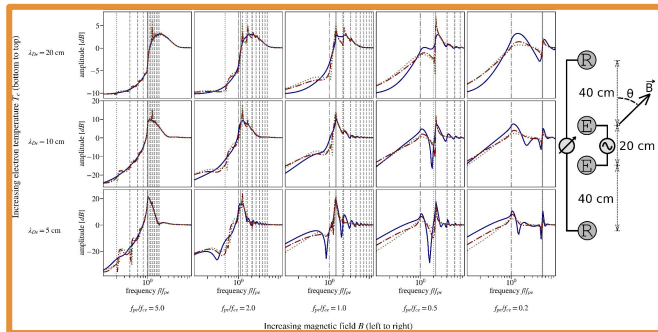
The fitted plasma parameters obtained from our model are in agreement with the ones measured by the WIND/3DP instrument

- $T_{e,c}$ cold electron temperature
- $n_{e,c}$ cold plasma density
- $T_{e,h}$ hot electron temperature
- $n_{e,h}$ hot plasma density
- B magnetic field

“Diagnostic of density(s) and electron temperature(s) in magnetized plasma using mutual impedance and quasi-thermal noise experiments.”

Mutual impedance in magnetized plasma

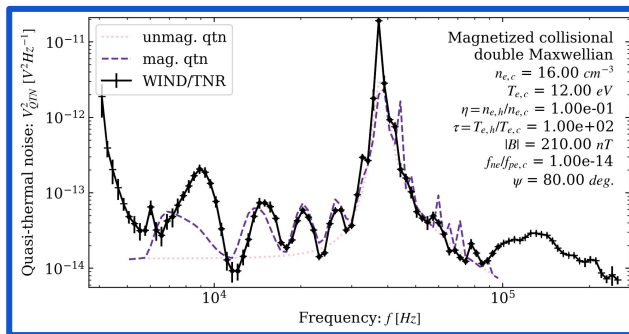
$$\frac{V}{V_0} = \frac{\sqrt{r^2 + z^2}}{\pi} \int_0^{+\infty} dk_r \int_0^{+\infty} dk_z \frac{k_r J_0(k_r r) \cos(k_z z)}{k^2 \varepsilon_L(k_r, k_z, \omega)}$$



T_e electron temperature
 n_e plasma density
 B magnetic field
 $T_{e,\perp}/T_{e,\parallel}$ electron temperature anisotropy

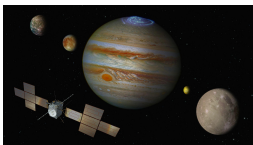
Quasi-thermal noise in magnetized plasma

$$|V_{QTN}(\omega)|^2 = C_i \int_0^{+\infty} \int_0^{+\infty} \frac{k_{\perp}}{k^4} \frac{F_{a,red} R_{f,N}}{|\varepsilon_L|^2} dk_{\parallel} dk_{\perp}$$



$T_{e,c}$ cold electron temperature
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 $T_{e,h}$ hot electron temperature
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